



Defence Research and
Development Canada

Recherche et développement
pour la défense Canada



Complexity and Chaos - State-of-the-Art; Formulations and Measures of Complexity

*M. Couture
DRDC Valcartier*

Defence R&D Canada – Valcartier

Technical Note

DRDC Valcartier TN 2006-451

September 2007

Canada

Complexity and Chaos - State-of-the-Art; Formulations and Measures of Complexity

M. Couture
DRDC Valcartier

Defence R&D Canada – Valcartier

Technical Note
DRDC Valcartier TN 2006-451
September 2007

Principal Author

Mario Couture
Defence Scientist

Approved by

Guy Turcotte
Head/System of Systems Section

Approved for release by

This work is part of project 15bp01 – Defensive Software Design.

- © Her Majesty the Queen in Right of Canada, as represented by the Minister of National Defence, 2007
- © Sa Majesté la Reine (en droit du Canada), telle que représentée par le ministre de la Défense nationale, 2007

Abstract

Different formulations and measures that may be used for evaluating the complexity of systems are gathered in this Technical Note. They might be useful for describing aspects of military complex systems. They were extracted from documents issued from the scientific literature dedicated to Complexity Theory, chaos and complex systems.

Résumé

Différentes formulations et mesures qui peuvent être utilisées pour évaluer la complexité des systèmes sont rassemblées dans ce document. Ces formulations et mesures peuvent être utiles pour décrire différents aspects des systèmes militaires complexes. Elles ont été extraites de documents provenant de la littérature scientifique traitant de la théorie de la complexité, du chaos et des systèmes complexes.

This page intentionally left blank.

Table of contents

Abstract	i
Résumé	i
Table of contents	iii
List of figures	vi
List of tables	vii
Acknowledgements	viii
1 Introduction.....	1
1.1 Context and Scope of this Document	1
1.2 The Used Methodology	1
1.3 How to use this Document	3
2 Formulations and Measures of Complexity.....	5
2.1 Abstract Computational Complexity	5
2.2 Algorithmic Complexity.....	5
2.3 Algorithmic Information Complexity.....	5
2.4 Arithmetic Complexity	6
2.5 Bennett's 'Logical Depth'	6
2.6 Cognitive Complexity	7
2.7 Computational Complexity	8
2.8 Connectivity	8
2.9 Crutchfield's Topological Complexity.....	8
2.10 Cyclomatic Complexity.....	8
2.11 Cyclomatic Number.....	8
2.12 Descriptive/Interpretative Complexity	9
2.13 Dimension of Attractor.....	9
2.14 Ease of Decomposition.....	10
2.15 Economic Complexity	10
2.16 Effective Measure Complexity.....	10
2.17 Entropy	10
2.18 Goodman's Complexity	11
2.19 Hieratical complexity.	11
2.20 Hinegardner and Engelberg's Number of Parts Definition.	11
2.21 Horn Complexity	12
2.22 Image complexity	12
2.23 Information complexity	12
2.24 Information Gain in Hierarchically Approximation and Scaling	13
2.25 Irreducibility.....	14

2.26	Kauffman's complexity.....	14
2.27	Kemeny's Complexity	14
2.28	Kolmogorov complexity.....	14
2.29	Layout Appropriateness.....	15
2.30	Length of Proof.....	15
2.31	Logical Complexity/Arithmetic Hierarchy.....	15
2.32	Logical depth.....	15
2.33	Loop Complexity.....	15
2.34	Low Probability	16
2.35	Minimum Number of Sub Groups.....	16
2.36	Minimum Size	16
2.37	Mutual Information	17
2.38	Network Complexity	17
2.39	Number of Axioms	18
2.40	Number of Dimensions.....	18
2.41	Number of Inequivalent Descriptions.....	18
2.42	Number of Internal Relations	19
2.43	Number of Spanning Trees.....	19
2.44	Number of States in a Finite Automata	19
2.45	Number of Symbols.....	20
2.46	Number of Variables	20
2.47	Organised/Disorganised Complexity.....	20
2.48	Pattern complexity.....	20
2.49	Shannon Information & Concept of Entropy	21
2.50	Simplicity	21
2.51	Size, Number of Parts.....	21
2.52	Size of Grammar.....	22
2.53	Size of matrix	22
2.54	Sober's Minimum Extra Information.....	22
2.55	Sophistication	23
2.56	Stochastic Complexity.....	23
2.57	Structural Complexity	23
2.58	Structure density.....	23
2.59	Syntactic Depth	24
2.60	Tabular Complexity.....	24
2.61	Time and Space Computational Complexity.....	24
2.62	Topological complexity.....	25
2.63	Tulis' Display complexity.....	25
2.64	Variety	26

3 Conclusion	27
References	28
Annex A Edmonds' List of References (Edmonds, 1999)	29
Bibliography	60

List of figures

Figure 1 The Methodology Used in this Work.....	2
---	---

List of tables

Table 1 List of Documents Issued from this Work.	3
---	---

Acknowledgements

The author would like to thank Mister Robert Charpentier from DRDC Valcartier for his support during all this work.

1 Introduction

This document contains the results of numerous searches that were made in the context of a state-of-the-art in the domain of the Complexity Theory, chaos and complex systems. It aims at regrouping together current ways of formulating and measuring complexity of complex systems.

1.1 Context and Scope of this Document

This document is the second of a set of five DRDC Valcartier reports dedicated to the study of complexity theory, chaos and complex systems (Couture, 2006a, 2006b, 2006c, 2006d, and one to be published in 2007). It is part of an overarching project being carried on at DRDC Valcartier, Project 15bp01 – Defensive Software Design. It focuses mainly on the presentation of concepts from this theory. There are only a few references to the architecting and engineering aspects of complexity. These aspects will be covered in another document.

1.2 The Used Methodology

Figure 1 depicts the general methodology used for this study. It is characterized by a main iterative and incremental loop (steps 1 and 2), which includes a number of sequential and parallel activities (steps 3, 4 and 5). This loop permits on-the-fly adjustment and optimization.

The five main activities or steps are:

1. **Search literature, projects, groups, etc:** Internet searches were made using Google and other search engines. A number of specialized databases were also searched (Dialog Database Catalog, 2005). These databases are listed in Annex C of Couture (2006a).
2. **Select potentially useful documents:** Documents were selected based on their potential applicability to the military context.
3. **Study selected documents:** Approximately 30–40% of the selected documents were read and studied in greater detail.
4. **Investigate in greater depth for the military context:** This involved finding elements that offer potential solutions in the military context.
5. **Update documents:** The content of each document was updated on the fly at each iteration.

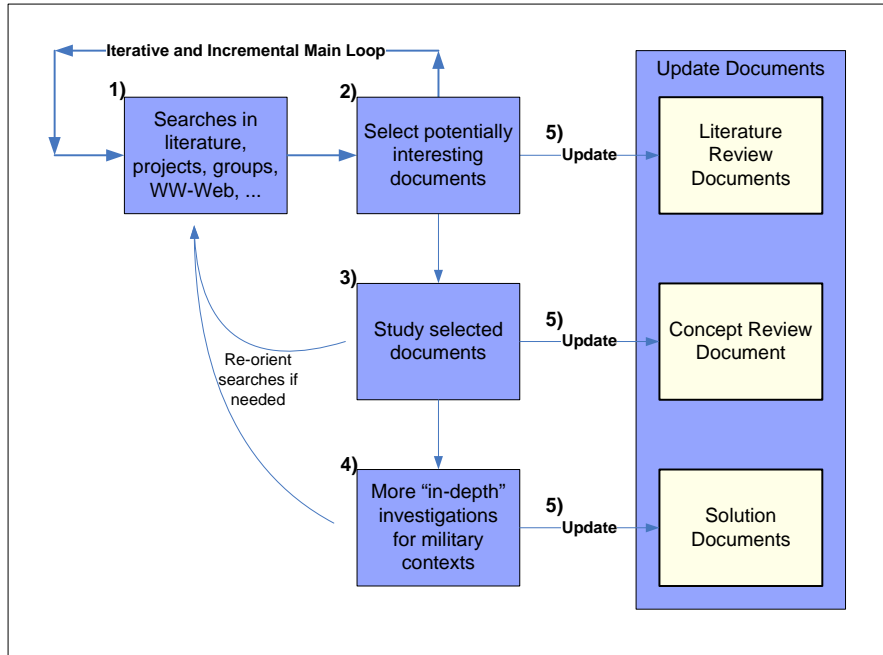


Figure 1 The Methodology Used in this Work.

The reports generated by this study are listed in Table 1. The first four reports will be published by the end of phase one of the study (by March 2007). The last will be published by the end of phase two (late 2007).

Table 1 List of Documents Issued from this Work.

Title	Description
<p>Complexity and chaos – State-of-the-art; List of works, experts, organizations, projects, journals, conferences and tools.</p> <p>(Couture, 2006a).</p>	<p>This Technical Note provides 471 references to scientific studies, organizations, scientific journals, conferences, experts and tools, plus 713 additional Internet addresses that are related to complexity theory, chaos and complex systems. Abstracts are included where available.</p>
<p>Complexity and chaos – State-of-the-art; Formulations and measures of complexity.</p> <p>(This document).</p>	<p>Different formulations and measures of system complexity are provided in this Technical Note. They were drawn from the scientific literature on complexity theory, chaos and complex systems.</p>
<p>Complexity and chaos – State-of-the-art; Glossary.</p> <p>(Couture, 2006c).</p>	<p>This Technical Note defines 335 key words related to complexity theory, chaos and complex systems. The definitions were extracted from the scientific literature.</p>
<p>Complexity and chaos – State-of-the-art; Overview of theoretical concepts.</p> <p>(Couture, 2007).</p>	<p>This Technical Memorandum presents an overview of theoretical concepts pertaining to complexity theory.</p>
<p>Complexity and chaos – State-of-the-art; The Engineering of complex adaptive systems.</p> <p>(To be published in 2007).</p>	<p>Descriptions of the current approaches, methodologies and tools used to address problems related to the architecting, engineering and improvement of complex systems is included in this Technical Report.</p>

1.3 How to use this Document

This report is a starting point reference for the search of information related to the current ways to formulate and measure the complexity of systems. Considering the quantity of information included in this document, three ways of searching are proposed:

- **To get a general survey on a specific subject:** The reader may simply use the Table of Content for locating specific subjects.
- **To find specific information on a specific subject:** The reader must use its word processor's search engine to find all appearances of selected key words within this

document. S/he will also find appropriate key words and addresses that can be re-used in further searches over the Internet for instance.

- Edmonds' list of references is also an important source of information (Edmonds, 1999). The reader is invited to refer to this important PhD Thesis.

2 Formulations and Measures of Complexity

This Chapter contains a number of 64 formulations/measures of complexity for complex systems pertaining to different domains or disciplines. A copy of Edmonds' list of 500 references (Edmonds, 1999) has been included in Annex A in order to facilitate the finding of cited documents.

2.1 Abstract Computational Complexity

(Edmonds, 1999): *Blum [67] proposed an abstract definition of computational complexity. If $\pi_i(n)$ are the functions representing the computation of the programs P_i , then $c_i(n)$ are a set of complexity measures iff $c_i(n)$ is defined exactly when $\pi_i(n)$ is defined and the predicate $c_i(n)=m$ is decidable. This definition neatly includes the time and space measures as well as many other sensible resource measures (such as the number of jumps executed) and is strong enough to prove many of the important theories concerning them. However this definition is too broad as it allows measures which don't obey the subprogram property (if P is a program that first applies a subprogram Q to an input and then a subprogram R to the result, then the complexity of P should be at least as great as that of Q or R). Thus according to this approach you get programs with more complex subprograms. Fixes for the abstract definition of computational complexity are suggested by Turney in [444, 445, 446], and Ausiello suggests a weakened version in [31]. [66] argues that computational complexity should be extended over other fields like the real numbers.*

2.2 Algorithmic Complexity

(Flake, 1998): *The size of the smallest program that can produce a particular sequence of numbers. Regular patterns have low algorithmic complexity and random sequences have high algorithmic complexity.*

2.3 Algorithmic Information Complexity

(Edmonds, 1999): *The Algorithmic Information Complexity (AIC) of a string of symbols is the length of the shortest program to produce it as an output. The program is usually taken as running on a Turing Machine. It was invented by Solomonoff [419], Kolmogorov [266] and Chaitin [99, 100, 101] separately, although perhaps anticipated by Vitushkin (section 8.45 on page 161). It has been one of the the most influential complexity measures (along with that of computational complexity) and has inspired many variations and enhancements including 'sophistication' (section 8.42 on page 159), and 'logical depth' (section 8.4 on page 138). Although Solomonoff considered it as a candidate for selection amongst equally supported scientific theories (i.e. a measure of simplicity – section 8.37 on page 156), Kolmogorov and Chaitin considered it as a measure of information (see section 8.15 on page 144 and section 8.24 on page 149). It has many interesting formal properties [99], including: 1. The more ordered the string, the shorter the program, and hence less complex. 2. Incompressible strings (those whose programs are not shorter than themselves) are indistinguishable from random strings. 3. Most long strings are incompressible. 4. In a range of formal systems you can't prove (within that*

system) that there are strings above a certain fixed level of complexity (derived basically from the AIC of its axioms). 5. In general it is uncomputable. Property 2 illustrates the deep connection between AIC and disorder. This is particularly evident in physics where a very close connection between Algorithmic complexity and entropy has been shown [449], to the extent that it is often referred to as an entropy. Property 4 indicates that the AIC complexity is more of an information measure. While one might believe that it is not possible to produce more information within a formal system than is encoded by the axioms, it would be extremely counter-intuitive if there was a limit to how complex one could prove strings in it to be. AIC has been applied in many ways: to define randomness in a non-probabilistic way [309, 499]; to capture descriptive complexity [293] (see also section 8.8 on page 141); Rissanen uses a statistical version to motivate a principled trade-off between the size of model and its error in [377, 378, 379]; to biological complexity [203, 223, 345]; to cognitive models [397]; economic models [452] and data compression [499]. Lempel-Ziv encoding can be seen as a computable approximation to it [279, 495]. Given that it is better characterised as an information measure rather than complexity, it has very close connections with entropy, as explored in [169, 420, 496, 497]. It is generalised in [80]. Good summaries of the many formal results and applications can be found in [40, 41, 70, 118, 286]. Other formal results include [80, 284, 456, 451, 494]. A summary of philosophical applications can be found in [285], with others in [102, 301, 469].

(Sommerer and Mignonneau, 2002): *The best-known definition of complexity is the Kolmogorov-Chaitin-Solomonoff (KCS) definition [62], describing Algorithmic Information Complexity (AIC), which places complexity somewhere between order and randomness; that is, complexity increases as P_{min} , the shortest algorithm that can generate a digit sequence, S , increases to the length equal to the sequence to be computed; when the algorithm reaches this incompressibility limit the sequence is defined as random. The KCS definition distinguishes between “highly ordered” and “highly complex” structures.*

2.4 Arithmetic Complexity

(Edmonds, 1999): *This is the minimum number of arithmetic operations needed to complete a task. This is important in order to make computational algorithms more efficient, for example Strassen [424] improved upon Gauss's method for solving linear equations from operations to $C \times n^{2.71}$. This is more of a practical definition and not intended as a general model of complexity. The operations of arithmetic are very particular. It also does not take into account the precision of the operations or of rounding errors. A summary of the theory of the arithmetic hierarchy can be found in [178].*

2.5 Bennett's 'Logical Depth'

(Edmonds, 1999): *Bennett [54, 55, 56] defines 'logical depth' as the running-time to generate the object in question by a near-incompressible program. Strictly the depth of a string x at level s is: $D_s(x) = \min \{T(p) \mid p \text{ is a program of length } \leq s \wedge U(p) = x\}$, where p ranges over programs, $T(p)$ is the time taken by program p , p^* is the smallest such program and U is a universal Turing computer. He states that this is intended as a measure of the value of information. For example, tide-tables can have a greater value than the equations which were used to calculate them as a lot of useful computation has been done. Thus he says [57]: “Logically deep objects... contain internal evidence of having been the result of a long computation or slow-to-simulate dynamically process and could not*

plausibly have originated otherwise.”. The plausibility of its origin comes from the assumption that the most likely program to produce an output would be the shortest one. This idea comes from Solomonoff. He justifies this as a physically plausible measure of complexity by its obedience to the “slow growth law” of complexity. This informal law states that complexity can only arise slowly through stochastic processes, as presumably has occurred in evolution. By its construction one cannot produce a deep object from a shallow one by a deterministic process and only improbably by a stochastic one. Thus random strings and very simple ones both have a low logical depth. A random string is incompressible and hence the minimal program that produces it, is a simple copying program, which is quick. A simple pattern can be produced by a simple program, and so will also be fairly quick. Koppel [268] shows that Logical Depth is the same as Sophistication (section 8.42 on page 159) for infinite strings.

2.6 Cognitive Complexity

(Edmonds, 1999): *In cognitive psychology, several types of complexity are distinguished. The most discussed of these is Cognitive Complexity. This was defined by Kelly as a part of his theory of personality [250]. He developed his ‘role construct repertory’ test to test it. Since then it has been used as a basis for discussion on the complexity of personal constructions of the real world (and particularly of other people) in psychology. It asks the subjects to rate a number of people known to them (e.g. closest friend of same sex) on a number of attributes (like Outgoing vs. Shy). The dimension of the inferred mental model of these people is then estimated as their cognitive complexity. So, for example, people who assign to all their friends positive attributes and to their enemies negative attributes would have a one-dimensional mental model of their acquaintances, as everybody is aligned along this good/friend - bad/enemy scale. Such people are said to be “cognitively simple”. A person who indicated that some of both their friends and enemies were good and bad would have at least a two-dimensional model with people placed across a good-bad, friend-enemy pair of axes. This person would have a higher score and would be called “more cognitively complex”. Thus the level of cognitive complexity indicates the number of potential relationships between the various attributes. Quite a number of variations of this has been suggested to capture this idea [404]. Unfortunately these seem to measure slightly different things as they do not correlate in practice [204], although they do have some robustness over time [342]. There does not seem to be any strong connection between cognitive complexity and IQ [95], innovation [187], intellectual sophistication [416], loquacity [81] or educational level [366]. It does seem to have some relation to the ability to use complex language [48, 409]. The application of hierarchically structured algorithmic information is discussed in [397]. A synthesis of several measures of cognitive complexity is suggested in [413] in the internal representation used by subjects. Other related measures include: [59, 382, 426].*

(Xing and Manning, 2005): *Another line of complexity studies involves cognitive complexity. While complexity studies generated by information theory focus on the complexity of a system itself, studies of cognitive complexity focus on observers: complexity from the perspective of the observer, i.e., the users. Since air traffic control involves cognitive tasks such as monitoring the situation, resolving conflicts, issuing instructions, etc., it is important to understand how cognitive complexity is measured to assess the complexity of ATC displays. Cognition may best be thought of a construct system composed of constructs and elements (Kelly 1955). The constructs are transparent templates that a person uses to comprehend the world. In a sense then, humans create the templates and fit the perception of the world to them.*

2.7 Computational Complexity

(Sommerer and Mignonneau, 2002): *Computational complexity is now a much studied area with many formal results [66]. The foundation of complexity theory is the research into computability theory undertaken since the 1930s onward by Alan Turing, Alonzo Church and Stephen Kleene [67], among others. The primary considerations then were the formalization of the notion of a computer (e.g. the Turing machine, Church's lambda calculus) and whether such a computer could solve any mathematical problem.*

2.8 Connectivity

(Edmonds, 1999): *The greater the extent of inter-connections between components of a system, the more difficult it is to decompose the system without changing its behaviour. Thus the connectance of a system (especially when analysed as a graph [367]) becomes a good indication of the potential for complex behaviour, in particular the likelihood that the system will achieve an equilibrium. The connectivity of a system has been variously measured, including the number of relations (section 8.30 on page 153) and the cyclomatic number (section 8.7 on page 140). Applications include: the reliability of circuits [470]; the stability of random linear systems of equations [25]; stability in computational communities [259]; stability in ecosystems [86, 227, 353]; the diversity of ecosystems [308]; the structure of memory [273]; logical and computational properties of bounded graphs [319]; competition in networks [373]; random digraphs [405]; chemical reaction mechanisms [491]; and general emergent behaviour in biological systems [197].*

2.9 Crutchfield's Topological Complexity

(Sommerer and Mignonneau, 2002): *The topological complexity described by James Crutchfield [65] is a measure of the size of the minimal computational model (typically a finite automaton of some variety) in the minimal formal language in which it has a finite model. Thus the complexity of the model is "objectivized" not only by considering minimal models but also as related to the nested hierarchy of formal languages.*

2.10 Cyclomatic Complexity.

(Xing and Manning, 2005): *McCabe (1976) defined cyclomatic complexity as the difference between the total number of transitions and the total number of states.*

2.11 Cyclomatic Number

(Edmonds, 1999): *The most basic graph measure (apart from the number of vertices) is the cyclomatic number of the graph. This is basically the number of independent loops in a graph. It is easily calculated by the formula $n(G) = m - n + p$, where m is the number of arcs, n the number of vertices and p the number of disjoint partitions the graph divides into. This intuitively captures the inter-connectedness of a graph or system; a hierarchically structured machine is completely predictable (a tree has no loops), whilst one with many feedback loops can exhibit more complex*

behaviour. An army is organised on hierarchical lines, presumably to simplify the chain of command to make it more predictable and hence more controllable. On the other hand, a creative committee meets to allow the maximum number of communication channels to enable the unpredictable to occur. In general there is no direct relation between the size (number of nodes) and the (cyclomatic) complexity. If a system is represented by a graph with the presence of some relation indicated by an arc, then the number of nodes will limit the cyclomatic complexity. This effect is only significant with very few nodes as the number of possible arcs goes up exponentially with the number of nodes. For the theory of this area see [436] McCabe [313] uses this as a measure of program complexity, in particular to calculate the number of different logical paths through a program to gauge how many tests it might need. Other applications include: complexity of simulation models [403]; and the difficulty of software maintenance [49, 125, 232]. For discussion on this see section 5.4 on page 106.

2.12 Descriptive/Interpretative Complexity

(Edmonds, 1999): *Löfgren [293] writing from a biological and psychological context, distinguishes between descriptive and interpretative complexities. In a system with a description (like DNA) and its realisation (the proteins in the cell), he associates his two measures of complexity with the two processes of interpretation and description. That is the complexity of encoding the realisation into a descriptive code and decoding it back into a realisation of that code. Löfgren chooses Kolmogorov complexity (section 8.2 on page 136) for the process of description and an ordering based on logical strength (section 8.20 on page 146) for the interpretative complexity.*

(Sommerer and Mignonneau, 2002): *In 1969, Ronald Fagin decided to study spectra (the spectrum of a first-order sentence is the set of cardinalities of its finite models) and Asser's problem (1955): "Is the class of spectra closed under complementation?" [68] In 1970, his investigations expanded to generalized spectra (i.e. existential second-order spectra where not all relation symbols are quantified out). Fagin's most important result was probably his characterization of NP as the class of generalized spectra in 1974. Interest in the subject has now exploded, mainly due to the intimate relationship (first hinted at by Fagin) between finite model theory and complexity theory [69]. In fact, there is an established subject area within finite model theory dealing explicitly with this relationship: descriptive complexity theory.*

2.13 Dimension of Attractor

(Edmonds, 1999): *Chaotic processes are difficult to model. A small change in state now causes a large change later which makes it impossible to predict the exact state beyond a certain time limit. This does not mean that all aspects of the process are impossible to model. It is possible to estimate the processes' attractor in state space; this is often fractal with chaotic processes. The dimension of the attractor is a measure of how complex the process is. Depending on the method of convergence for the calculation of a dimension for the attractor you get a slightly different measure. These, in fact, form a sequence of dimensions. For an accessible introduction see Baker [39].*

2.14 Ease of Decomposition

(Edmonds, 1999): *The ease with which a system can be decomposed into sub-systems has close connections with the “analytic complexity” of section 5.2 on page 87. The general area is covered by [18, 110, 144, 338, 421]. Some techniques for systematic decomposition are: the use of a matrix algorithm to plan the use of multiplexers for circuits [278]; a graphical approach in [242]; decomposing difference equations [30, 306]; a hierarchical holographic algorithm [72]; the design of decision support facilities [225]; a systems approach [157]; and a technique based on whether data relations commute [131]. The converse of and complement to decomposability is reconstructability analysis [94].*

2.15 Economic Complexity

(Edmonds, 1999): *“Complexity” in economics, frequently means merely that some of the usual simplifying assumptions do not hold. An example of these assumptions is that an agent acts as if it can infer the action to perfectly optimise its utility. This goes back to Simon’s distinction between procedural and substantive rationality [415]. See the paper in Appendix 7 - Complexity and Economics, for a full discussion of the concept of complexity in economics. Some papers that cover this are [10, 14, 20, 172, 173, 200]. In game-theory, there has been some more direct formulation of actual complexity measures, including: a critique of the “number of states” measure [43] (section 8.32 on page 153); the information of strategies [290]; a survey of the area [229]. Another area deals with choice processes, including: the group-theoretic complexity of decision rules [163]; a survey of choice processes and complexity [192], the computability of choice functions [251]; hierarchies [484]; and the cardinality of collections of decisions [52].*

2.16 Effective Measure Complexity

(Sommerer and Mignonneau, 2002): *Peter Grassberger [75] defines the Effective Measure Complexity (EMC) of a pattern as the asymptotic behavior of the amount of information required to predict the next symbol to the level of granularity. EMC can be seen as the dif. culty of predicting the future values of a stationary series, as measured by the size of regular expression of the required model. A similar approach is taken by Badii and Politi.*

2.17 Entropy

(Edmonds, 1999): *In physics, entropy measures the level of disorder in a thermodynamic system. The more disordered it is, the more information is needed to describe it precisely. In particular systems with very low entropy are simple to describe (they don’t move around a lot). Thus complexity and entropy can be associated, although this was not intended by its originators [408]. Entropy based measures are essentially probabilistic. The Boltzman-Gibbs-Shannon entropy is most frequently used in physics, but Algorithmic Complexity can also be used if the complexity of the whole ensemble is low [497]. The principle of maximum entropy [282] has been used to help formalise complexity [114, 156, 171]. Entropy based measures have often been used as measures of complexity including: the regularity in noisy time series [354]; the topology of chemical reactions [492]; coalitions of economic agents [452]; physical computation [496]; the difficulty of system diagnosis [183]; artificial life [371]; and the complexity of graphs [332].*

2.18 Goodman's Complexity

(Edmonds, 1999): *Goodman [186] has devised an elaborate categorisation of extra-logical predicates, based on expressiveness. For example, a general predicate is deemed more complex than a symmetric one, as it includes the later as a specific example. Likewise a three place predicate is more complex than a two place one. Goodman builds upon this starting point. The idea is that when faced with two theories that have equal supporting experimental evidence one should choose the simpler one using this measure. The complexity of a complex statement is merely the sum of the complexities of its component predicates, regardless of the structure of the statement. It is similar in spirit to Kemeny's measure (section 8.18 on page 146). A recent defence and reformulation of this idea has been made by Richmond in [376].*

(Sommerer and Mignonneau, 2002): *Nelson Goodman [71] has devised an elaborate categorization of extra-logical predicates based on expressiveness. For example, a general predicate is deemed more complex than a symmetric one, as it includes the later as a speci. c example. Likewise, a three-place predicate is more complex than a two-place one. Goodman builds upon this starting point. The idea is that, when faced with two theories that have equal supporting experimental evidence, one should choose the simpler one using this measure. The complexity of a complex statement is merely the sum of the complexities of its component predicates, regardless of the structure of the statement.*

2.19 Hieratical complexity.

(Xing and Manning, 2005): *This definition is also concerned with structural rules. A complex system is often constructed hierarchically. That is, it is composed of structures on several scales or levels. These may be scales of space or time, or levels within a domain-specific functional space. For example, an ATC display may be composed of several windows, consisting of different types of text and graphical regions, and each text region (such as a datablock) containing several types of information. With this in mind, Bates and Shepard (1993) assumed that a system is composed of elementary units with local structures and the interconnections between the local structures are governed by rules. They suggested that complexity is manifested as variability in the convergence and divergence of interconnections. Then the dimensionality of local structures, number of local structures, and the range of connections all contribute to the global complexity. Moreover, if local regions possess certain computational abilities, then multiple regions can interact to achieve greater complexity.*

2.20 Hinegardner and Engelberg's Number of Parts Definition.

(Sommerer and Mignonneau, 2002): *Perhaps the simplest measure of complexity is that suggested by R. Hinegardner and H. Engelberg [63]: the number of different parts. Hinegardner and Engelberg's measure evokes "exploded" diagrams of pieces of machinery. They give some indication of complexity, but leave out what is perhaps most important: "organization" and "levels of organization" [64].*

2.21 Horn Complexity

(Edmonds, 1999): *The Horn complexity of a propositional function is the minimum length of a Horn formula (in its working variables) that defines that function. This was defined by Aanderaa and Börger [1] as a measure of the logical complexity of Boolean functions. It is polynomially related to the network complexity [2], described below (section 8.26 on page 151).*

(Sommerer and Mignonneau, 2002): *The Horn complexity of a propositional function is the minimum length of a Horn formula (in its working variables) that defines that function. This was defined by S.O. Aanderaa and Egon Börger [73] as a measure of the logical complexity of Boolean functions. It is polynomially related to network or circuit complexity, which is the minimum number of logical gates needed to implement a logical function [74].*

2.22 Image complexity

(Xing and Manning, 2005): *A digital image is numerically specified; thus, the information content can be easily computed using information theory. Many algorithms have been developed to compute image complexity. The standard Boltzmann-Gibbs entropy measure defines complexity with respect to a given size of a window of view. According to the definition, image complexity, measured as configurational entropy, is a function of the total number of distinguishable spatial arrangements within view windows of a given size. The statistical paradigms based on this measure have shown great success in quantifying image complexity. However, experiments have shown that information complexity computed in term of entropy does not correspond to perceived complexity. While entropy is a measure of image disorder and reflects the lack of spatial homogeneity, complexity is a combination of order and disorder. Indeed, Grassberger (1986, 1991) has shown that complexity is sometimes posited as a mid-point between order and disorder.*

2.23 Information complexity

(Edmonds, 1999): *The amount of information a system encodes or the amount of information needed to describe a system has a loose connection with its complexity. As noted above, there is a close connection between the amount of information and disorder. Using the Algorithmic Complexity (section 8.2 on page 136) measure of information, disordered patterns hold the most information, patterns encoding the maximum amount of information are indistinguishable from random patterns. Information can be measured deterministically using algorithmic information complexity (section 8.2 on page 136) or probabilistically using entropy (section 8.12 on page 143). Either of these can be used to define mutual information (section 8.25 on page 151). See also section immediately below (section 8.16 on page 145). Klir exhibits an axiomatic framework for complexity similar to those I list in section 5.2 on page 87, combined with the requirement that complexity should be proportional to the information required to resolve any uncertainty [262, 263, 264, 265]. This may be seen as a formulation of Waxman's "problem complexity" [463]. A number of approaches which seek to combine elements of both algorithmic and Shannon information include: [170, 378, 452, 496]. Computational complexity has been extended to cover information flow by adding a cost function to the information used by a computation [440, 441, 442]. Applications include: charting the increase in information in the evolution of finite*

automata [26, 27]; the fluctuation of information in 1-D automata [47]; its connection with logical depth in evolution [53]; its connections to computational complexity [138]; the connection between various measures of information via random vectors [144]; the regularity of short noisy chaotic series [160]; error-prone sections of programs by potential information flow [214, 277]; systems problem solving [262]; the classification of strategies in repeated games [290]; the estimation of the information of a pattern [340]; and a principle of the minimum increase in evolution [399].

(Xing and Manning, 2005): Complexity has been extensively studied within the field of information theory, where the term “information complexity (IC)” is frequently used to describe complexity from the perspective of a system. There have been many attempts to quantify IC theoretically. Below we list some widely used complexity measures. These measures do not necessarily exclude each other. Instead, they emphasize different aspects of complexity and are somewhat complementary.

- Kolmogorov complexity.
- Topological complexity.
- Mutual information.
- Logical depth.
- Kauffman’s complexity.
- Hierarchical complexity.

2.24 Information Gain in Hierarchically Approximation and Scaling

(Edmonds, 1999): Attention in physics has focused on the complexity of chaotic physical processes with a fractal nature, where one gets different behaviours at different levels of granularity. In 1986 Grassberger introduced “Effective Measure Complexity” [193], which measured the asymptotic increase in information with increased scale. He develops this in [194, 195]. Badii, Politi and others [33, 34, 35, 36, 130] use trees of increasingly detailed Markov models to approximate a growing pattern. Each branch off a node is a possible extension of the pattern that may follow. He then defines the complexity of the pattern as the (Shannon) information gain in each level over the size of the tree at the level, taking the limit at infinitely many levels. Any Markov process has zero complexity. This is to reflect the difficulty in predicting complex systems. The class of easily predicted systems that Badii focuses on are those which exhibit different behaviours at different levels of detail. He says “A system is complex if it reveals different laws (interactions) at different resolution (coarse grinning) levels.”. [202] argues that these measures assume that the process is stationary, i.e. is basically a Markov process and [457] classifies them according to whether they are based on homogeneous or generated partitions and whether they are based on dynamic or structural elements. Other papers in this area include: [3, 7, 28, 29, 350, 480, 490]. A good review of this whole area is [36].

2.25 Irreducibility

(Edmonds, 1999): *Holists often use the word “complexity” for that which is irreducible [339] (at least by current practice). This is, in a sense, an extreme case of the difficulty of decomposition (section 8.10 on page 142). Such approaches include: [13] where the importance of size to qualitative behaviour is pointed out; [468] which argues that the evolution of multiple and overlapping functions will limit reduction in biology; [11] which discusses the application to public policy in forestry; [247] which charts how chaos challenges the reductionist approach; [257] which applies this to modelling organisations; as a result of self-organisation [205]; the incompatibility of information and computation [243]; as a result of the epistemic cut between syntax and semantics [347]; number of elements an instance of a pattern must consist of to exhibit all the characteristics of a class [210]; and [323] which discusses Rosen’s approach [384, 389] and relates this to the “sciences of complexity”. This approach to complexity seems particular to biology, for general surveys of the connection of complexity with holism see [244, 348, 388, 481]. Some suggest that this may be due to using the wrong formal language for modelling, including [74, 167, 246, 244, 330, 344, 410, 482, 488].*

2.26 Kauffman’s complexity.

(Xing and Manning, 2005): *Kauffman (1993) defined complexity as the “number of conflicting constraints.” The definition represents the difficulty of specifying a successful task within the constraints or “rules” imposed. For example, an airspace can be made less complex by removing air traffic constraints such as military zones, bad weather, etc. Note, however, that the definition is only concerned with the complexity factor of structural rules.*

2.27 Kemeny's Complexity

(Edmonds, 1999): *In the field of “simplicity”, Kemeny [254] attributes an integral measure of complexity to types of extra-logical predicates. He does it on the basis on the logarithm of the number of non-isomorphic finite models a predicate type has. On the basis of this he gives extra-logical predicates a complexity which could be used to decide between equally supported theories. This is similar in style and direction to Goodman’s measure in section 8.13 on page 143.*

(Sommerer and Mignonneau, 2002): *In the field of “simplicity,” John G. Kemeny [72] attributes an integral measure of complexity to types of extra-logical predicates, on the basis of the logarithm of the number of non-isomorphic . nite models that a predicate type has. On the basis of this he assigns to extra-logical predicates a measured complexity ranking that could be used to decide between equally supported theories. This is similar in style and direction to Goodman’s measure above.*

2.28 Kolmogorov complexity

(Xing and Manning, 2005): *According to information theories, the most straightforward definition of complexity is the minimum description size. Hence Kolmogorov complexity is defined as the minimum possible length of a description in some language (Casti, 1979). For instance, if*

a description can be greatly compressed without loss of meaning, then it is considered simpler than one that cannot. By this definition, highly ordered expressions appear as simple and random while maintaining maximal complexity.

2.29 Layout Appropriateness

(Xing and Manning, 2005): *Tullis' metrics are task independent. They are focused on the general appearance of an interface. Therefore, it is more useful for predicting user preference than user performance other than search time. In contrast, task-sensitive metrics are more useful in understanding what users do with an interface and how to make the interface more efficient. For instance, Sears (1994) proposed a measure, called Layout Appropriateness, to evaluate the efficiency of the organization of objects in an interface. This metric first computes the cost of a layout using the following formula: Cost = sum (frequency of transition × cost of the transition).*

2.30 Length of Proof

(Edmonds, 1999): *Simpler theorems, on the whole, need shorter proofs. On the other hand longer proofs are tedious to follow. Thus it is natural to search for short proofs (e.g. as in [96]). One can arbitrarily lengthen almost any proof. This alone makes length alone as a measure of complexity unsatisfactory. Some short “elegant” proofs are very complicated and some careful long explanatory proofs easy to follow. For this measure to make any sense needless length needs to be eliminated (see minimum size measures in section 8.24 on page 149). Other papers touching on this include: [180, 209].*

2.31 Logical Complexity/Arithmetic Hierarchy

(Edmonds, 1999): *Mathematical proof theorists classify mathematical objects and processes according to the projective hierarchy (sometimes called the arithmetic hierarchy). Girard [178] surveys this area thoroughly. [107] shows that the arithmetic complexity of the problem of deriving a word from a fixed starting point is arbitrarily more complicated than the word problem itself.*

2.32 Logical depth.

(Xing and Manning, 2005): *Logical depth is defined as the computational cost (time and memory) taken to calculate the shortest program that can reproduce a given object (Bennett, 1990). By this definition, complexity is the difficulty of computation from a random starting point to the resulting state. This measure is aimed at the complexity of the process and not the results. That is, it is a combination of both storage and computational power.*

2.33 Loop Complexity

(Edmonds, 1999): *The loop complexity of a primitive recursive function is the iteration depth of the primitive recursive register operators in its definition. Thus $x+1$ would be level 0, $x+y$ level 1 (as it can be defined recursively from $x+1$), x^y level 2 etc. This can be used to define a hierarchy*

of sets $LOOP_n$ of functions with loop complexity not greater than n [322]. This is one of the large collections of measures used to predict the maintainability of software, for a survey of these see [498].

2.34 Low Probability

(Edmonds, 1999): *The connection of probability and complexity is intricate. The probability of a highly ordered complex system arising by chance is low, hence sometimes complexity is associated with low probability [136]. On the other hand if complexity is conflated with informational measures such as entropy (section 8.12 on page 143) or algorithmic information (section 8.2 on page 136) then complexity is associated with high probability. This has led many to look for other measures such that complex systems will lie between order and disorder including those in section 8.16 on page 145 and section 8.46 on page 161. In the contrary direction the philosophy of “simplicity” (section 6.5 on page 129 and section 8.37 on page 156) has led to the identification of a higher a priori probability of the truth of a theory with a lack of complexity. That this is mistaken see the arguments in section 6.5 on page 129 and the paper in Appendix 6 - Complexity and Scientific Modelling. An application of low probability to the difficulty of system diagnosis is in [183].*

2.35 Minimum Number of Sub Groups

(Edmonds, 1999): *The Krohn-Rhodes prime decomposition theory [17, 272] tells us that we can decompose any semi-group into a wreath product of alternating simple groups and semi-groups of order 3. There are decompositions which are minimal in terms of the number of such alternations, i.e. they have the least number of groups in their decomposition. The number of such groups is called the complexity of the original group. If you take the product of a group with another group then the result will be more complex, which accords with our intuitions.*

2.36 Minimum Size

(Edmonds, 1999): *As discussed in section 3.4.3 on page 58, minimum size overcomes some of the inadequacies of mere size as a complexity measure. It avoids the possibility of needless length and is nicely independent of the particular expression chosen. It would correspond to using a perfectly efficient language, the occurrence of any redundancy in a specific expression was eliminated by perfect compression. However the minimum size of a particular representation can still be a largely accidental feature of the description process. Different ideas are sometimes more succinctly expressed in different languages (natural and formal). For example, to express a conjunction in a negation-implication fragment of classical propositional logic is necessarily longer than that for implication itself. This would not mean that implication was simpler than conjunction. Minimum size also ignores any question of inter-relatedness or relevance. Compare the cases of 1001 inter-related facts about logic and 1001 unrelated general knowledge facts (presuming this to be possible). It is probably possible to compress the 1001 inter-related facts more than the unrelated ones because the very fact of their relatedness indicates a degree of redundancy. The minimum size approach to complexity would thus attribute a lower complexity to the 1001 related facts but few would say these were less complex. What is true is that the system of unrelated facts holds more information but is far complex (as a system). In a way that is*

similar to what occurred for length measures, some of these seem to have had the label “complexity” applied post-hoc, so it is difficult to judge how seriously they were meant as a complexity measure. The most frequent special case of a minimum size measure is Algorithmic Information which corresponds to a minimal sized Turing Machine (see section 8.2 on page 136), but other minimum size approaches are also used with other formal languages, in particular finite automata (see section 8.32 on page 153), this approach is criticised in [43] for the analysis of equilibria in repeated games. Crutchfield generalises the minimal size criterion over the whole formal language hierarchy, so that complexity is the minimal size in the “lowest” formal language for which this is finite [121]. He contrasts this complexity measure with a version of effective measure complexity (section 8.16 on page 145) which he calls “statistical complexity” [123]. The method for finding such an expression is given in [119] and applied to the process of modelling chaotic process in [120, 121]. Minimum size measures have also been applied to capture the static complexity of cellular automata in [472]; and to a minimal complexity in evolution [296].

2.37 Mutual Information

(Edmonds, 1999): *If you have defined an entropy like measure (e.g. Shannon Entropy or Algorithmic Complexity), $H(A)$ and from that a joint entropy $H(A;B)$ which is the entropy of A and B joined, then you can define. This can be interpreted as, i.e. the extent of the shortening when considered together rather than separately. A high mutual information between remote parts of a system can indicate a closely connected or self-similar system. The connectiveness in such a system can be the cause of its complexity. Bennett [55] points out that this arises for rather different reason in equilibrium and non-equilibrium systems. In equilibrium situations the mutual information comes from the intervening medium (like in a gas), in non-equilibrium systems it must come from some other connection. He points out that simple operations like duplicating and mixing up random bits of DNA generate large amount of remote non-equilibrium mutual information. [287] shows that past-future mutual entropy is not related to entropy in a straight-forward manner. [7] formulates “physical complexity” as the mutual information (defined relative to a Landauer-Turing Machine) between a systems and its universe. Mutual information has been applied to capture some of the dynamic complexity of cellular automata in [289].*

(Xing and Manning, 2005): *Complexity is indicated by levels of mutual information that measure the correlation between information at sites separated by time and space (Langton, 1991). This definition describes the computational power requirement. For example, if each controller only needs to handle aircraft within one’s sector regardless of traffic in the next sector, the task would be less complex because traffic in the next sector is not relevant to his or her problem space.*

2.38 Network Complexity

(Edmonds, 1999): *Network or circuit complexity is the minimum number of logical gates needed to implement a logical function [400]. This is very difficult to compute in most cases but some upper and lower limits can be proved. This measure depends on the choice of logic gates that you can use to build the circuits from. This measure has an immediate importance for electronic engineers who seek to minimise the expense of logic gates as in [278]. This is polynomially*

related to Horn Complexity (section 8.14 on page 143). For surveys of results in this field see [40, 142, 400].

2.39 Number of Axioms

(Edmonds, 1999): Meredith and Lukasiewicz both put considerable effort into finding small axiom sets for classical propositional logic. However it is far from obvious that this is helpful. The axiom has no immediately comprehensible meaning and it makes for an incredibly tortuous proof theory. For more on this see section 5.6.1 on page 113.

2.40 Number of Dimensions

(Edmonds, 1999): In any model of a process, the number of dimensions it takes is of critical importance. A necessarily high dimensional model has the potential for great complexity. Conversely if there is a simple relationship between dimensions in a model you can often reduce the models dimension by forming composite dimensions with out any loss of descriptive power. Hence if a model is necessarily of high dimension then there is no very simple relationship between any of its several dimensions, i.e. the model must be reasonably complex. This has been applied to concept learning [298]; the performance of connecting networks [307] and in cognitive complexity (section 8.5 on page 139). Fractal dimension is used to measure plant development in [113].

2.41 Number of Inequivalent Descriptions

(Edmonds, 1999): If a system can be modelled in many different and irreconcilable ways, then we will always have to settle for an incomplete model of that system. In such circumstances the system may well exhibit behaviour that would only be predicted by another model. Thus such systems are, in a fundamental way, irreducible. Thus the presence of multiple inequivalent models are considered by some as the key characteristic of “complexity”. These people are usually holists, namely [323, 389]. See also section 4.3.1 on page 83. This approach can be extended in restricted circumstances to measuring complexity by the number of inequivalent descriptions [88, 89].

(Sommerer and Mignonneau, 2002): If a system can be modeled in many different and irreconcilable ways, then we will always have to settle for an incomplete model of that system. In such circumstances, the system may well exhibit behavior that would only be predicted by another model. Thus such systems are fundamentally irreducible. Accordingly, the presence of multiple inequivalent models has been considered by Robert Rosen [76] and Howard Pattee [77] as the key characteristic of complexity. Casti [78] extends this approach and defines complexity as the number of nonequivalent descriptions that an observer can generate for a system with which he or she interacts. The observer must choose a family of descriptions of the system and an equivalence relation among them— the complexity is then the number of equivalence classes the family breaks down into, given the equivalence relation.

2.42 Number of Internal Relations

(Edmonds, 1999): *If one is focusing on the topology of a model, then one improvement on the simple size of the network as an indication of its complexity is the number of relations indicated between the nodes. Rouse and Rouse [392] in their study of the time taken to complete tasks found a strong correlation between the time taken to perform fault diagnosis tasks with complex relations and the number of internal relations in that circuit (represented by a wiring connection). Van Emden [450] examines the mathematics of a variety of entropic measures based on the information indicated by the internal relations at different levels.*

2.43 Number of Spanning Trees

(Edmonds, 1999): *An interesting graphical measure is the number of spanning trees of a graph (see also section 8.7 on page 140). A spanning tree is a subgraph with no loops which includes all the vertices. The number of spanning trees grows very fast with the cyclomatic number and size of the graph. A tree has only one spanning tree [252]. [58] applies this to a classification of games. [226, 237] use such trees as the basis for a measure of complexity to capture the variety in the structure of trees.*

2.44 Number of States in a Finite Automata

(Edmonds, 1999): *Much formal work [231] has been done on the number of states of finite automata. In these works this number is frequently taken as the complexity (e.g. [164]). Again it is easy to elaborate a model by adding redundant states, a difficulty which is circumvented by selecting a minimal or “acceptable” model (see section 8.24 on page 149 above). Gaines [165] is pessimistic about a useful general theory of complexity, saying: “The ordering of models in terms of complexity is arbitrary and depends upon our individual points of view.”, and again: “When we specify an order relation upon the models we may find that the behaviours of many important systems require complex models under our ordering, whereas, with a different ordering on the same class of models, they all become simple.”. He, nonetheless, introduces the useful concept of admissibility (borrowed from statistics [465]) and applies it to the search for simple finite-state automata for various string patterns. He uses a working definition of complexity which counts the number of states of an automaton and then goes on to identify, with the help of the program ATOM, admissible models of various sizes. Here models are said to be admissible if any other model that gives a better approximation of the behaviour is more complex (in the sense of number of states). In [164] he shows that even a small amount of randomness can cause an indefinite increase in an induced automata model. This work is extended in [396] to stochastic automata. Von Neuman speculated that there was a critical threshold which allowed self-reproduction [454]. In [303] it is shown that Turing machines with very few states can exhibit complex behaviour. Complexity as the number of states in a finite automata has been widely applied: to characterise the emerging complexity resulting from the actions of cellular automata [289, 472, 473, 474, 476]; in economic game theory [229]; to characterising social structure [9] and in characterising the computation done in chaotic systems [122].*

2.45 Number of Symbols

(Edmonds, 1999): *The number of symbols is not a reliable guide to complexity. Merely to count the number of symbols in philosophical works would give one little indication of their complexity.*

2.46 Number of Variables

(Edmonds, 1999): *The number of variables in a statement can have an immediate impact both on proofs that use it and the complexity of its models. Both of these effects depend on the structure of the statement. For example the axiom $a \rightarrow b$ has a catastrophically simplifying effect on both proofs and models compared to that of $a \rightarrow a$. As with the number of symbols (section 8.33 on page 154 above) the number of variables can have a limiting effect on complexity but the number of variables is not a sufficient condition for complexity. Diamond and McKinsey proved [139] that for a broad range of logics you need at least one axiom with three variables in it.*

2.47 Organised/Disorganised Complexity

(Edmonds, 1999): *Weaver [464] classified scientific problems into the simple, and the complex. Then he further classified the complex problems into those of disorganised complexity and organised complexity. Simple problems are those with a few variables like the path of a billiard ball and a complex problem is one with many variables like a gas. Disorganised complexity is typified by many independent variables, so that it is amenable to statistical techniques. Examples of this are the properties of a gas or a nation's accident statistics. Organised complexity occurs when "There is a sizeable number of factors which are interrelated into an organic whole" Examples given by him include the immune system of animals and economic fluctuations.*

2.48 Pattern complexity

(Xing and Manning, 2005): *Unlike Boltzmann-based complexity, pattern complexity of an image is based on measures of visual features. Orland et al. developed an algorithm to measure pattern complexity (Orland, Weidemann, Larsen, & Radja, 1994). Pattern complexity includes measures of color, edges, fractal dimensions, deviation and entropy. While the measure is somewhat correlated to human judgment of image appearance, it is not a solid predictor of perceived complexity. Klinger and Salingaros (2000) proposed a pattern complexity index based on the following visual features: size, density, line curvature, color, symmetry, similarity of shapes, and correctness of form. In their algorithm, complexity is composed of two components: Harmony and Temperature. Harmony H measures the correlation of subunits via symmetries; Temperature T measures symbol variation. The temperature components for complex structures were: 1) intensity and size of details; 2) differentiation density; 3) line curvature; 4) color-intensity; and 5) color-contrast. Harmony is a similar five-part sum composed of the following symmetry values: 1) vertical and horizontal reflections; 2) translations and rotations; 3) shape-similarity; 4) form-connectedness; and 5) color-matching. Pattern complexity can then be computed as $C = T (H_{max} - H)$.*

2.49 Shannon Information & Concept of Entropy

(Edmonds, 1999): *Although Shannon [408] did not envisage his measure of information being used to quantify complexity, some of his successors have either used it as such or based complexity measures upon it. The Shannon measure of information is a statistical measure based on the probability of receiving a message. If $p(m_1)$, $p(m_2)$, ... are the probabilities of receiving the messages m_1 , m_2 , ... then the information carried by the message n_1 , n_2 , ... is defined as $-SUM_i(\log_2(p(n_i)))$. The more improbable the message, the more information it gives the recipient. See the section on information (section 8.15 on page 144) and entropy (section 8.12 on page 143).*

(Sommerer and Mignonneau, 2002): *Shannon Entropy [70] can be seen as the difficulty of guessing the content of a message passing down a channel, given the range of possible messages. The idea is that the more difficult it is to guess, the more information a message holds. This concept was not intended as a measure of complexity, but has been used as such by subsequent authors.*

2.50 Simplicity

(Edmonds, 1999): *When faced with two theories which are equally supported by the available experimental evidence, it is natural to choose the simpler of the two. Further than this, when a theory has been elaborated in order to explain the evidence, it is often fruitful to search for a simpler theory. The study of the grounds for choosing between equally supported theories has acquired the label “Simplicity” (see [4, 78, 186, 253, 254, 339, 485]). From the point of view of theories about the world, all purely logical propositions are equally and ultimately certain and hence “simple”. Thus measures of simplicity do not help us to distinguish between logical theories, they were not meant to. Many theories of Simplicity have chosen grounds other than simplicity as the criterion for choosing between equally supported theories, e.g. Popper's refutability [358] or Defrays [241] identification of Simplicity with high probability. Some theories with connections with complexity are Goodman's (section 8.13 on page 143), Kemeny's (section 8.18 on page 146) and Sobers (section 8.41 on page 158). For a fuller discussion of this see section 6.5 on page 129 and Appendix 6 - Complexity and Scientific Modelling.*

2.51 Size, Number of Parts

(Edmonds, 1999): *There is clearly a sense in which people use “complexity” to indicate the number of parts but seems rarely used just to indicate this. It would be odd for a person opening a phone book or a large box of matches to exclaim “Oh, how complex!”. Contrast these examples with those of a mathematical text book or an intricate (old fashioned) watch, where this would be more appropriate. Size seems not to be a sufficient condition for complexity. On the other hand a certain minimum size does seem to be a necessary condition for complexity. It is very hard to imagine anything complex made of only two parts. However, this minimum size can be quite small: small non-abelian mathematical groups can be very complex indeed as are many other formal systems with a sparse axiomatisation. The rate of potential complexity seems to increase very fast with size. This does not, of course, mean that all large systems are complex. Size based measures of complexity seem to come about in two circumstances: as a result of a post-hoc*

labelling of a formal device (as in simple induction proofs where the length of a proof, the number of connectives or the depth of nesting is in need of a convenient label) and to indicate a potential for complexity (as in the number of variables in a formula). Anderson points out that size can make a qualitative difference to the behaviour of systems [13] as [454] also suggests, but [303] indicates that in the presence of powerful inferential machinery that the critical size can be very small. Applications include: the social organisation and community size [83]; the minimum number of gates in a circuit [278]; the cyclical behaviour of systems [458]; self-replicating sequences [44]; rule-based systems [341]; neural networks and cellular automata [188]; and grammatical development [256]. See also the discussion in section 3.4.1 on page 57 and the other size and numerosity based approaches in this appendix.

2.52 Size of Grammar

(Edmonds, 1999): A pattern, if viewed as the result of production rules in a language, has a grammar [231]. In general the simpler the pattern, the simpler the grammar. So the size of the grammar gives us a handle on the complexity of the pattern. The size and complexity Syntactic of the grammar can vary depending on what sort of language you are assuming the pattern to be a representative of. For instance Gaines [164] shows that the assumption that a process can be modelled by a deterministic finite automaton leads to very large models (proportional to the length of the evidence) in the presence of even a small amount of indeterminism. This measure would identify all patterns of a particular language as equally complex unless the pattern happens also to be a member of another language as well. Sahal [396] demonstrates similar results, but with stochastic automata. Frequently the size of grammar is taken relative to a Turing machine (section 8.2 on page 136) or finite automata (section 8.32 on page 153). Other approaches include simple depth (section 8.44 on page 160) or star height in regular languages [153]. Applications include: biological macromolecules [146]; chaotic systems in physics (section 8.16 on page 145); and communication complexity [235].

2.53 Size of matrix

(Edmonds, 1999): The size of a minimal characteristic matrix for a logic is an indication of the logic's complexity [209]. Classical logic has the smallest possible matrices (2x2), and more complex logics like R, do not have finite characteristic matrices at all. This measure is an indication of the the complexity of logic's semantics but does not have a direct relationship with the complexity of its proof theory (see section 5.6.2 on page 117). This sort of approach has been applied to: the stability of computational communities [259]; flow dominance in layout problems [215]; and hierarchical decomposition of systems [72].

2.54 Sober's Minimum Extra Information

(Edmonds, 1999): In the field of the “simplicity” of scientific theories, Sober [418] rejected the idea of an absolute measure in favour of that of an ordering based on how much extra information would be needed to select an answer to a particular question: this is implicitly as relativised informativeness. Thus simplicity was to be relative to a question (represented by a set of possible answers). The theory that needs the least minimum extra information to select an answer to the question is deemed the simpler one. When one is judging theories with respect to a

number of questions one must decide a weighting of the relative importance of the questions, to decide the overall simplicity. Sober applies this to mathematical and logical fields by examining how the fundamental axioms are chosen. This is done by seeing how much information they contribute to the question of whether the axiom is true in our world or not. According to Sober “This mirrors our belief that a contraction in the axiom set is a gain in simplicity. Moreover, a proof that the axioms are mutually independent is a proof that the axiom set is maximally simple; no axiom is redundant. And a proof that the axiom set is complete simplifies our view of the area being axiomatised, for it assures us that relative to the axiom set, every truth is redundant.” Next Sober considers some logical properties of (extra-logical) relations by considering the informativeness of them relative to the general question of whether two objects are related. Thus he arrives at similar conclusions to Goodman (e.g. a symmetrical relation is simpler than an anti-symmetrical one etc.).

2.55 Sophistication

(Edmonds, 1999): Koppel [268] defines “sophistication” as a measure of the structure of a string. He says: “The minimal description of a string consists of two parts. One part is a description of the string's structure, and the other part specifies the string from among the class of strings sharing that structure (Cover 1985). The sophistication of a string is the size of that part of the description which describes the strings structure. Thus, for example, the description of the structure of a random string is empty and thus, though its complexity is high, its sophistication is low.”

2.56 Stochastic Complexity

(Edmonds, 1999): Rissanen [379] finds the idea of “shortest code length” (like algorithmic complexity) attractive but difficult to apply when modelling physical processes. He estimates the minimum code length of data encoded with a probabilistic model, using Shannon's coding theory. This can be seen as a statistical and computable version of algorithmic information (section 8.2 on page 136) as well as an attempt to establish a principled trade-off between a model's complexity and error rate (see Appendix 6 - Complexity and Scientific Modelling). Re-christened as the minimum description length (MDL) principle [378], it has been successfully applied to machine learning [377, 493].

2.57 Structural Complexity

(Xing and Manning, 2005): In simplest terms, absolute structural complexity equals the number of states (Stevens, Myers, & Constantine, 1974). Relative structural complexity is the ratio of the number of transitions to the number of states, i.e., the number of transitions per state.

2.58 Structure density.

(Xing and Manning, 2005): Kornwachs (1987) proposed “structure density” as a measure of system complexity. This measure estimates the actual density of transitions compared with the maximal possible density. Let S be the number of all possible states of a system and T be the number of actual transitions. The maximal possible number of transitions is $S * (S-1)$. Then the

structure density is defined as $T/(S*(S-1))$. By this definition, the structure density of the above example is $4/(3*(3-1))=0.66$.

2.59 Syntactic Depth

(Edmonds, 1999): *The deeper phrases are embedded in a statement (according to some syntax), the more difficult they are to understand. Identifying the ease of comprehension is one of the primary purposes of measures of syntactic complexity in formal language theory. In 1960 Yngve [483] proposed depth of postponed symbols as a measure of syntactic complexity, this was criticised by Miller and Chomsky [326] on formal grounds. They preferred the degree of self-embedding because it was "... precisely the property that distinguishes context-free languages from the regular languages." Other measures proposed in [383] include depth and nesting. The depth of a syntactic expression is the maximum number of arcs from root to leaf when represented in a tree form. This has nothing to do with either "logical depth" (section 8.4 on page 138) or "thermodynamic depth" (section 8.46 on page 161). From the point of view of a modeller, depth is a useful way to stratify a space of expressions in a recursive language, as typically the number of possible expressions goes up exponentially with the depth. Although as [349] points out this could be done in any number of ways. Thus depth is relevant to the problem of induction whether by humans (see section 6.5 on page 129 and Appendix 6 - Complexity and Scientific Modelling) or in machine learning [111, 148, 333]. Syntactic depth as an indication of complexity has also been applied to menu design [239]; the difficulty of resolution of ambiguity [174] and circuit design [355, 356].*

2.60 Tabular Complexity

(Edmonds, 1999): *Tabular complexity is an adaptation of Kolmogorov's e-entropy [267] by Vitushkin [453]. It is a measure of the complexity of finite-state automata (see also section 8.32 on page 153). To calculate it one takes the tables representing the change of state and the output of the semi-group of the states of the automata and then decomposes these tables into smaller sub-tables, also allowing for the decomposition of the "wiring" (the connections) between these sub-tables etc. The minimum total volume obtainable is the tabular complexity, i.e. it is the volume of the most compact tabular representation. Thus tabular complexity is similar to It is only applicable to processes modellable by finite automata (a proper subset of those computable by a Turing Machine). The tabular complexity can be very difficult to calculate but estimates can be produced by exhibiting specific tables.*

2.61 Time and Space Computational Complexity

(Edmonds, 1999) *Computational complexity is now a much studied area with many formal results. It is usually cast as the order of the rate of growth of the resources needed to compute something compared to the size of its input. Such time and space complexity measures are the most studied computational measures. Articles which include the word complexity often refer to these. They reflect the degree of effort required to compute a problem, independent of particular instances of that problem. They are fairly rough measure because they only give the degree of increase to within a constant factor, e.g. the order of the polynomial with which they increase. This is because of possible variations in the abstract computer that does the calculation. Several*

variations of this have been proposed, including: extension to other fields like the real numbers [66]; continuous complexity models [318]; information based complexity (which adds a cost function to the information used) [440, 441, 442]; and using uniform rather than logarithmic size [211]. Applications include: social choice theory [251]; grammatical inference [155]; learning [184]; simplification in logic [315]; feasibility of reasoning by a limited agent [281]; communication [235]; induction [111]; simulation [335]; control theory [486, 487]; perceptrons [500]; improving performance on 3-SAT problems [230]; and propagation in boolean circuits [425]. Summaries of the field can be found in [40, 41, 70].

2.62 Topological complexity.

(Xing and Manning, 2005): Crutchfield and Young (1989) extended the concept of Kolmogorov complexity by defining complexity as the minimal size of a model representation of a system that can statistically reproduce the observed data within a specified tolerance. Consider, for example, two air traffic cases. In the first case, ten aircraft are flying on two fixed routes that have one intersection. In the second case, ten aircraft are flying off the routes, which can create many potential conflicts. A controller can build a model of the first case that has two flows of aircraft and one crossing point, while a model of the second case has to be composed of many flows and crossings. Thus the topological complexity of Case A is less than Case B. This definition takes into account both the minimal size and the fixed hierarchy or structural rules of a system. One shortcoming of the definition is that it does not provide a unique measure of complexity for a system because there is not necessarily a “minimal” model for it (Pressing, 1999). That is, users may construct different models of the same system. In addition, neither this nor the definition above is sufficient to describe complexity because they only emphasize the storage resource that it takes to solve a class of problems.

2.63 Tullis' Display complexity

(Xing and Manning, 2005): Perhaps the most useful tool to quantify the information and layout of screen elements is Tullis' metric of display complexity (Tullis, 1984, 1985, 1986). Tullis studied over a thousand computer-generated displays. He measured search time to locate items on the displays and collected subjective ratings of ease of use. The results revealed that four basic characteristics of display formats affect how well users can extract information from the displays:

1. Overall density — the number of characters displayed, expressed as a percentage of the total spaces available.
2. Local density — the number of other characters near each character.
3. Grouping — the number of groups and average group size, both describing the extent to which characters on the display form perceptual groups. The groups can be determined by considering the white space around them.
4. Layout complexity — the extent to which the arrangement of items on the display follows a predictable visual scheme, typically computed as the differences in view angles between the items.

2.64 Variety

(Edmonds, 1999): *A complex system is likely to exhibit a greater variety in terms of its behaviour and properties. Thus variety is an indication of complexity (though not always as sometimes a very complex system is necessary in order to maintain equilibrium). Variety can be measured by the simple counting of types, the spread of numerical values or the simple presence of sudden changes. In this way it overlaps with information (section 8.15 on page 144) and entropic (section 8.12 on page 143) measures. Applications include: punctuated behaviour [38]; stability of ecosystems [353]; competing behaviours and control [357]; tree structures [237]; number of inequivalent models [89]; the interaction of connectivity and complexity [218]; and evolution [316].*

3 Conclusion

A number of 64 different ways of formulating complexity are listed and briefly described in this document. While this list is not complete it provides the reader a first reference for finding most currently used key words on this subject. By using proposed searching methods described in Chapter 1, the reader will then be able to find the needed information 1) in this document; 2) in Edmonds (1999); or 3) over Internet.

References

Couture, Mario, 2006a. Complexity and Chaos – State-of-the-Art; List of Works, Experts, Organizations, Projects, Journals, Conferences and Tools. DRDC/RDDC Valcartier Technical Note Number TN 2006-450. Defence R&D Canada, Valcartier, Quebec, Canada.

Couture, Mario, 2006c. Complexity and Chaos – State-of-the-Art; Glossary. DRDC/RDDC Valcartier Technical Note Number TN 2006-452. Defence R&D Canada, Valcartier, Quebec, Canada.

Couture, Mario, 2006d. Complexity and Chaos – State-of-the-Art; Presentation of Theoretical Concepts. DRDC/RDDC Valcartier Technical Memorandum TM Number 2006-453. Defence R&D Canada, Valcartier, Quebec, Canada.

Dialog Database Catalog, 2005. 2005 Database Catalog. Dialog, a Thomson Business, West Group, Eagan, Mn, USA, publication Number GSM-05-20001 (<http://www.dialog.com>).

Edmonds, Bruce, 1999. Syntactic Measures of Complexity. PhD Thesis. University of Manchester, number of pages: 254.

Flake, W. Gary, 1998. The Computational Beauty of Nature: Computer Explorations of Fractals, Chaos, Complex Systems, and Adaptation. The MIT Press, ISBN: 0262561271, number of pages: 514.

Sommerer, Christa and Laurent Mignonneau, 2002. Modeling the Emergence of Complexity: Complex Systems, the Origin of Life and Interactive On-Line Art. LEONARDO, Volume 35, Number 2.

Xing, Jing and Carol A. Manning, 2005. Complexity and Automation. Display of Air Traffic Control: Literature Review and Analysis. Final Report. Civil Aerospace Medical Institute, Federal Aviation Administration, Oklahoma City, OK 73125, Number of pages: 20.

Annex A Edmonds' List of References (Edmonds, 1999)

- [1] AADERAA, SO; BÖRGER, E. The Horn Complexity of Boolean functions and Cook's problem. In MAYOH, B; JENSEN, F (Eds). Proceedings of the 5th Scandinavian Logic Symposium. Aalborg: Aalborg University Press, 1979, 231-256.
- [2] AADERAA, SO; BRÖGER, E. The equivalence of Horn and network complexity of Boolean functions. *Acta Informatica*, 1981, 15, 303-307.
- [3] ABRAHAM, NB; ALBANO, AM; TUFILLARO, NB. Complexity and Chaos. In ABRAHAM, NB (Ed). *Measures of Complexity and Chaos*. New Jersey: Plenum Press, 1989, 1-25.
- [4] ACKERMANN, R. Inductive Simplicity. *Philosophy of Science*, 1961, 2, 152-160.
- [5] ACHINSTEIN, P. *Concepts of Science: A Philosophical Analysis*. Baltimore: Johns Hopkins Press, 1968.
- [6] ACHINSTEIN, P. History and Philosophy of Science: a reply to Cohen, P. In SUPPE, F (ed.). *The Structure of Scientific Theories*. Urbana, IL: University of Urbana Press, 1973, 350-360.
- [7] ADAMI, C; CERF, NJ. Complexity, Computation and Measurement. Fourth Workshop on Physics and Computation, Boston University, 1996. In TOFFOLI, T; BIAFORE, M; LEAO, J. *PhysComp96, NE: New England Complex Systems Institute*, 1996, 7-11.
- [8] AIDA, S et al. *The Science and Praxis of Complexity*. Tokyo: United Nations University, 1985.
- [9] ALBIN, PS. *The Complexity of Social Groups and Social Systems by Graph Structures*. *Mathematical Social Sciences*, 1980, 1, 101-129.
- [10] ALBIN, PS; GOTTINGER, HW. Structure and Complexity in Economic and Social Systems. *Mathematical Social Sciences*, 1983, 5, 253-268.
- [11] ALLEN, GM; GOULD, EM. Complexity, Wickedness and Public Forests. *Journal of Forestry*, 1986, 84, 20-23.
- [12] ANDERSON, AR; BELNAP, ND. *Entailment. The Logic of relevance and necessity, Vol. I*. Princeton: Princeton University Press, 1976.
- [13] ANDERSON, PW. More is Different. *Science*, 1972, 177, 393-396.
- [14] ANDERSON, PW; ARROW, KJ; PINES, D (Eds.). *The Economy as an Evolving Complex System*. Sante Fe, New Mexico: Santa Fe Institute, 1988. *Studies in the Sciences of Complexity*.

- [15] ANGELINE, PJ; KINNEAR, KE (eds.). *Advances in Genetic Programming, Volume 2*. Cambridge, MA: MIT Press, 1994.
- [16] APOSTEL, L. *Towards the Formal Study of Models in the Non-Formal Sciences*. *Synthese*, 1960, 12, 125-161.
- [17] ARBIB, MA (Ed.). *Algebraic Theory of Machines, Languages and Semigroups*. New York: Academic Press, 1968.
- [18] ARBIB, MA; MANES, EG. *Foundations of system theory: decomposable systems*. *Automatica*, 1974, 10, 285-302.
- [19] ARTHUR, B. *Why do things become more complex?* *Scientific American*, 1993, 268, 92.
- [20] ARTHUR, B. *Inductive Reasoning and Bounded Rationality*. *American Economic Association Papers and Proceedings*, 1994, 84, 406-411.
- [21] ARTHUR, WB. *On the Evolution of Complexity*. In COWNAN, G; PINES, D; MELTZER, D (Eds). *Complexity: Metaphors, Models and Reality*. Reading, MA: Addison-Wesley, 1994, 65-78.
- [22] ARTHUR, WB et al. (1996). *Asset pricing under endogenous expectations in an artificial stock market*. University of Wisconsin-Madison SSRI report 9625, 1180 Observatory Drive, Madison, WI 53706, USA
- [23] ASHBY, WR. *Introduction to Cybernetics*. New York: Methuen, 1964.
- [24] ASHBY, WR. *Some Peculiarities of Complex Systems*. *Cybernetic Medicine*, 1973, 9, 1-7.
- [25] ASHBY, WR; GARDNER, M. *Connectance of Large, Dynamic Cybernetic Systems: Critical Values for Stability*. *Nature*, 1970, 228, 784.
- [26] ATLAN, H. *Natural Complexity and the Self-Creation of Meaning*. In AIDA, et al (Ed). *The Science and Praxis of Complexity*. Tokyo: United Nations University, 1984, 173-192.
- [27] ATLAN, H. *The Self-Creation of Meaning*. *Physica Scripta*, 1987, 36, 563.
- [28] ATMANSPACHER, H; KURTHS, J; SCHEINGRABER, H; et al. *Complexity and meaning in nonlinear dynamical systems*. *Open systems and Information Dynamics*, 1992, 1, 269-289.
- [29] AUERBACH, D. *Dynamical Complexity of Strange Sets*. In ABRAHAM, NB (Ed). *Measures of Complexity and Chaos*. New York: Plenum Press, 1989, 203-207.
- [30] AUGER, PM. *Hierarchically Organized Systems - The Response to Complexity*. *Journal of Scientific & Industrial Research*, 1992, 51, 725-735.
- [31] AUSIELLO, G. *Abstract Computational Complexity and Cycling Computations*. *Journal of Computer and System Sciences*, 1971, 5, 118-128.

- [32] AYER, A. J. *Language, Truth and Logic*. London: Victor Gollanz, 1936.
- [33] BADII, R. *Unfolding Complexity in Nonlinear Dynamical Systems*. In ABRAHAM, NB et al (Ed). *Measures of Complexity and Chaos*. New York: Plenum Press, 1989, 313-325.
- [34] BADII, R. *Complexity and Unpredictable Scaling of Hierarchical Structures*. In BOUNTIS, T (Ed). *Chaotic Dynamics, Theory and Practice*. New York and London: Plenum Press, 1992, 1-19.
- [35] BADII, R; FINARDI, M; BROGGI, G. *Recursive symbolic Encoding and Hierarchical Description of Complex Systems*. In ATMANSPACHER, H; SCHEINGRABER, H (Eds). *Information Dynamics*. New York: Plenum Press, 1991, 35-43.
- [36] BADII, R; POLITI, A. *Complexity, Hierarchical Structures and Scaling in Physics*. Cambridge: Cambridge University Press, 1993.
- [37] BAIL, WG; ZELKOWITZ, MV. *Program complexity using hierarchical abstract computers*. *Journal of Computer Languages*, 1988, 13, 109-123.
- [38] BAK, P; PACZUSKI, M. *Complexity, contingency and criticality*. *Proceeding of the National Academy of Science USA*, 1995, 92, 6689-6696.
- [39] BAKER, GL. *Chaotic Dynamics*. Cambridge: Cambridge University Press, 1990.
- [40] BALCAZAR, JL. *Structural Complexity, Vol I*. Berlin: Springer-Verlag, 1990.
- [41] BALCAZAR, JL. *Structural Complexity, Vol II*. Berlin: Springer-Verlag, 1990.
- [42] BALDWIN, M. *Portraits of Complexity*. Ohio: Battelle Memorial Institute, 1975. Battelle Monographs.
- [43] BANKS, JF; SUNDARAM, RK. *Repeated Games, Finite Automata and Complexity*. *Games and Economic Behaviour*, 1990, 2, 97-117.
- [44] BANZHAF, W. *Self-Replicating Sequences of Binary Numbers: The Build-up of Complexity*. *Complex Systems*, 1994, 8, 215-225.
- [45] BAR-HILLEL, Y; KASHER, Y; SHAMIR, E. *Measures of Syntactic Complexity*. In BOOTH, AD (Ed). *Machine Translation*. Amsterdam: North-Holland, 1967, 30-50.
- [46] BARTLETT, S (Ed.). *Reflexivity: A source book in self-reference*. New York: Elsevier Science, 1992.
- [47] BATES, JE; SHEPARD, HK. *Measuring Complexity Using Information Fluctuation*. *Physics Letters A*, 1993, 172, 416-425.
- [48] BEATTY, MJ; PAYNE, SK. *Listening Comprehension as a Function of Cognitive Complexity*. *Communication Monographs*, 1984, 51, 85-89.

- [49] BECHIR, A; KAMINSKA, B. CYCLOGEN: Automatic, Functional-Level Test Generator Based on the Cyclomatic Complexity Measure and on the ROBDD Representation. *IEEE Transactions on Circuits and Systems - II: Analogue and Digital Signal Processing*, 1995, 42, 446-452.
- [50] BEDNARZ, J. Complexity and Intersubjectivity. *Human Studies*, 1984, 7, 55-70.
- [51] BEER, S. Managing Modern Complexity. *Futures*, 1970, 2, 245-257.
- [52] BEJA, A. Finite and Infinite Complexity in Axioms of Rational Choice or Sen's Characterization of Preference-Compatibility Cannot Be Improved. *Journal of Economic Theory*, 1989, 49, 339-346.
- [53] BENNETT, CH. Dissipation, Information, Computational Complexity and the Definition of Organization. In PINES, D (Ed). *Emerging Syntheses in Science*. Redwood city, CA: Addison-Wesley, 1985, 215-233.
- [54] BENNETT, CH. On the Nature and Origin of complexity in Discrete, Homogenous, Locally-Interacting Systems. *Foundations of Physics*, 1986, 16, 585-592.
- [55] BENNETT, CH. Information, Dissipation, and the Definition of Organization. In PINES, D (Ed). *Emerging Syntheses of Science*. Redwood City, California: Addison-Wesley, 1987, 256.
- [56] BENNETT, CH. Logical Depth and Physical Complexity. In HERKEN, R (Ed). *The Universal Turing Machine, A Half-Century Survey*. Oxford: Oxford University Press, 1988, 227-257.
- [57] BENNETT, CH. How to Define Complexity in Physics, and Why. In ZUREK, WH (Ed). *Complexity, Entropy and the Physics of Information*. Redwood City California: Addison-Wesley, 1990, 137-148.
- [58] BERLEKAMP, ER; CONWAY, JH; GUY, RK. *Winning Ways for Your Mathematical Plays*. New York: Academic Press, 1983.
- [59] BERLYNE, DE. Novelty, Complexity and hedonic value. *Perception and Psychophysics*, 1970, 8, 279-286.
- [60] BERRY, BJL. Comprehending Complexity. *Urban Geography*, 1994, 15, 695-697.
- [61] BETH, E. *Natuurphilosophie*. Gorinchen: Noordduyn, 1948.
- [62] BETH, E. Towards an Up-to-date Philosophy of the Natural Sciences. *Methodos*, 1949, 1, 178-185.
- [63] BETH, E. Semantics of Physical Theories. In FREUDANTHAL, H. (Ed.). *The Concept and the Role of the Model in Mathematics and Natural and Social Sciences*. Dordrecht: Reidel, 1961, 48-51.

- [64] BLACK, M. *Models and Metaphors*. Studies in Language and Philosophy. Ithaca, CA: Cornell University Press, 1962.
- [65] BLUM, L; BLUM, M. Toward a Mathematical Theory of Inductive Inference. *Information and Control*, 1975, 35, 125-155.
- [66] BLUM, L; CUCKER, F; SHUB, M; et al. *Complexity and Real Computation: A Manifesto*. *International Journal of Bifurcation and Chaos*, 1996, 6, 3-26.
- [67] BLUM, M. A Machine Independent Theory of the Complexity of Recursive Functions. *Journal of the Association of Computing Machinery*, 1967, 14, 322.
- [68] BOGEN, J; WOODWARD, J. Saving the Phenomena. *The Philosophical Review*, 1988, 98,:303-352.
- [69] BOHANEK, M; BRATKO, I. Trading Accuracy for Simplicity in Decision Trees. *Machine Learning*, 1994, 15, 223-250.
- [70] BÖRGER, E. *Computability, Complexity, Logic*. Amsterdam: North Holland, 1989.
- [71] BONNER, JT. *The Evolution of Complexity*. Princeton, NJ: Princeton University Press, 1988.
- [72] BOWDEN, K. Hierarchical tearing: an efficient holographic algorithm for system decomposition. *International Journal of General Systems*, 1994, 23, 23-37.
- [73] BRAITHWAITE, R. B. *Models in the Empirical Sciences*. In NAGEL, E; SUPPES, P; TARSKI, A (eds.). *Logic Methodology and the Philosophy of Science: Proceedings of the 1960 International Congress*. Stanford, CA: Stanford University Press, 1962, 224-239.
- [74] BREMERMAN, H. Algorithms, complexity, transcomputability and the analysis of systems. *Proceedings of the Fifth Congress of the Deutsche Gesellschaft für Kybernetik*, Munich (eds) Reidel,W, Handler,W Spreng,M, Oldenbourg, 1974.
- [75] BREMERMAN, H. Complexity of Automata, Brains and Behaviour. *Lecture Notes in BioMathematics*, 1974, 4, 304-331.
- [76] BREWER, GD. *Analysis of Complex Systems: An experiment and its implications for policy making*. Rand Corporation Report P-4951, Santa Monica, CA, 1973.
- [77] BROOKS, RJ; TOBIAS, AM. Choosing the best model: level of detail, complexity and model performance. *Mathematical and Computer Modelling*, 1996, 24, 1-14.
- [78] BUNGE, M. The Weight of Simplicity in the Construction and Assaying of Scientific Theories. *Philosophy of Science*, 1961, 28, 120-149.
- [79] BUNGE, M. *The Myth of Simplicity*. Englewood Cliffs: Prentice-Hall, 1963.

- [80] BURGIN, MS. Generalised Kolmogorov Complexity and other dual Complexity Measures. *Cybernetics*, 1990, 26, 481-491.
- [81] BURLESON, BR et al. More Evidence that Cognitive Complexity is Not Loquacity. *Communication Quarterly*, 34, 317-328
- [82] BURTON, M; DIRKIS, M. Defining Legislative Complexity - A Case study: the tax law improvement project. *University of Tasmania Law Review*, 1996, 14, 198-215.
- [83] CARNEIRO, RL. The Evolution of Complexity in Human Societies and its Mathematical Expression. *International Journal of Comparative Sociology*, 1987, 28, 111-128.
- [84] CARTWRIGHT, N. *How the Laws of Physics Lie*. Oxford: Oxford University Press, 1983.
- [85] CARTWRIGHT, N. Models: The Blueprints for Laws. *Philosophy of Science*, 1997, 64(proc), S292-S303.
- [86] CASTI, JL. Complexity, Connectivity and Resilience in Complex Ecosystems. *IFAC Symposium on Bio- and Ecosystems*, Liepzig, Germany, 1977.
- [87] CASTI, JL. *Connectivity, Complexity and Catastrophe*. NY: John Wiley, 1979.
- [88] CASTI, JL. On System Complexity: Identification, Measurement and Management. In CASTI, J; KARLQUIST, A (Eds). *Complexity Language and Life: Mathematical Approaches*. Berlin: Springer, 1986, 146-173.
- [89] CASTI, JL. The simply complex: trendy buzzword or emerging new science? *Bulletin of the Santa Fe Institute*, 1992, 7, 10-13.
- [90] CASTI, JL. What if. *New Scientist*, 1996, 151/2038, 36-40.
- [91] CASTI, JL; *Complexification*. London: Abacus, 1994.
- [92] CASTI, JL; KARQUIST, A (Eds.). *Complexity, Language and Life: Mathematical Models*. Berlin: Springer-Verlag, 1985.
- [93] CATTRELL, A. Emergent Properties of Complex Systems. In WESTON-SMITH (Ed). *The Encyclopedia of Ignorance*. Oxford: Pergammon, 1977, 129-135.
- [94] CAVALLO, RE; KLIR, GJ. Reconstructability Analysis: Overview and Bibliography. *International Journal of General Systems*, 1981, 7, 1-6.
- [95] CECI, SJ; LIKER,JK. A Day at the Races: A Study of IQ, expertise and cognitive Complexity, *Journal of Experimental Psychology (General)*, 115, 255-266.
- [96] CELLUCI, C. Proof Theory and Complexity. *Synthese*, 1985, 62, 173-189.
- [97] CHA, S; CHUNG, IS; KWON, YR. Complexity Measures for Concurrent Programs based on Information Theoretic Metrics. *Information Processing Letters*, 1993, 46, 43-50.

- [98] CHADWICK, GF. The limits of the plannable: stability and complexity in planning and planned systems. *Environment and Planning A*, 1977, 9, 1189-1192.
- [99] CHAITIN, GJ. On the Length of Programs for Computing Finite Binary Sequences. *Journal of the Association of Computing Machinery*, 1966, 13, 547-569.
- [100] CHAITIN, GJ. Algorithmic Information Theory. *IBM Journal of Research and Development*, 1977, 21, 350-9,496.
- [101] CHAITIN, GJ. Algorithmic Information Theory. Cambridge: Cambridge University Press, 1987.
- [102] CHAITIN, GJ. Randomness and Complexity in Pure Mathematics. *International Journal of Bifurcation and Chaos*, 1994, 4, 3-15.
- [103] CHAO, Y. R. Models in Linguistics and Models in General. In NAGEL, E; SUPPES, P; TARSKI, A (eds.). *Logic Methodology and the Philosophy of Science: Proceedings of the 1960 International Congress*. Stanford, CA: Stanford University Press, 1962, 558-566.
- [104] CHAPMAN, GP. The Epistemology of Complexity and some Reflections on the Symposium. In AIDA, et al (Ed). *The Science and Praxis of Complexity*. Tokyo: United Nations University, 1984, 357-374.
- [105] CHERNIAVSKY, JC; SMITH, CH. On Weyuker Axioms for Software Complexity Measures. *IEEE Transactions on Software Engineering*, 1991, 17, 636-638.
- [106] CLARKE, S; TOBIAS, AM. Complexity in Corporate Modelling: A Review. *Business History*, 1995, 37, 17-44.
- [107] COHEN, DE; MADLENER, K; OTTO, F. Separating the Intrinsic Complexity and the Derivational Complexity of the Word Problem for Finitely Presented Groups. *Mathematical Logic Quarterly*, 1993, 39, 143-157.
- [108] COHEN, PR. Heuristic Reasoning about Uncertainty: An Artificial Intelligence Approach. Boston, MA: Pitman, 1985.
- [109] COLLINS, AW. On the Question 'Do Numbers Exist?'. *Philosophical Quarterly*, 1998, 48, 23-36.
- [110] CONANT, RC. Detecting subsystems of a complex system. *IEEE Transactions on Systems, Man and Cybernetics*, 1972, 2, 550-553.
- [111] CONKLIN, D; WITTEN, IH. Complexity-Based Induction. *Machine Learning*, 1994, 16, 203.
- [112] COOPER, C. Complexity in C3I Systems. *Complexity International*, 1993, 1, 7.
- [113] CORBIT, JD; GARBARY, DJ. Fractal dimension as a quantitative measure of complexity in plant development. *Proceedings of the Royal Society of London B*, 1995, 262, 1-6.

- [114] CORNACCHIO, JV. Maximum Entropy Complexity Measures. *International Journal of General Systems*, 1977, 3, 267-271.
- [115] CORNACCHIO, JV. System Complexity - A Bibliography. *International Journal of General Systems*, 1977, 3, 267-271.
- [116] COTTRELL, A. Emergent Properties of Complex Systems. In DUNCAN, R; WESTON-SMITH, M (Eds). *Encyclopedia of Ignorance*. Oxford: Pergamon, 1977, 129-135.
- [117] COVENY, P; R. HIGHFIELD. *Frontiers of Complexity: the search for order in a chaotic world*. London: Faber and Faber, 1995.
- [118] COVER, TM. Kolmogorov Complexity, Data Compression, and Inference. In DURAND, H; DI LULLO, M; SINCLAIR, C (Eds). *The Impact of Data Processing Techniques on Communications*. Dordrecht: Nijhoff, 1983, 23-33.
- [119] CRUTCHFIELD, JP. Reconstructing Language Hierarchies. In ATMANSPACHER, H; SCHEINGRABER, H (Eds). *Information Dynamics*. New York: Plenum Press, 1991, 45-60.
- [120] CRUTCHFIELD, JP. Knowledge and Meaning... Chaos and Complexity. In LAM, L; NARODITSKY, V (Eds). *Modeling Complex Phenomena*. Berlin: Springer, 1992, 66-101.
- [121] CRUTCHFIELD, JP. Observing Complexity and The Complexity of Observation. In ATMANSPACHER, H (Ed). *Inside versus Outside*. Berlin: Springer, 1993, 235-272.
- [122] CRUTCHFIELD, JP. The Calculi of Emergence: Computation, Dynamics and Induction. *Physica D*, 1994, 75, 11-54.
- [123] CRUTCHFIELD, JP; YOUNG, K. Inferring Statistical Complexity. *Physics Review Letters*, 1989, 63, 105.
- [124] CUHROV, IP. On the Number of DNF Minimal Relatively Arbitrary Measures of Complexity. *Lecture Notes in Computer Science*, 1987, 278, 92-94.
- [125] CURTIS, B; SHEPPARD, SB; MILLIMAN, P; et al. Measuring the psychological complexity of software maintenance tasks with the Halstead and McCabe metrics. *IEEE Transactions on Software Engineering*, 1979, 5, 96-104.
- [126] CUSHING, J. T. Models and Methodologies in Current Theoretical High-Energy Physics. *Synthese*, 1982, 50, 5-101.
- [127] CUSHING, J. *Quantum Mechanics: Historical Contingency and Copenhagen Hegemony*. Chicago: Chicago University Press, 1994.
- [128] CUTLAND, NJ. *Computability*. Cambridge: Cambridge University Press, 1980.
- [129] DACOSTA, N. C. A; FRENCH, S. The Model-Theoretic Approach in the Philosophy of Science. *Philosophy of Science*, 1990, 57, 248-265.

- [130] D'ALESSANDRO, G; POLITI, A. Hierarchical approach to complexity with applications to dynamic systems. *Physics Review Letters*, 1990, 64, 1609-1612.
- [131] DAMPNEY, CNG; JOHNSON, SJ; DEUBLE, P. Taming Large Complex Information Systems. *Complex Systems* 92, Australia National University, 1993.
- [132] DANZIN, A. The Pervasiveness of Complexity: Common trends, New Paradigms, and Research Orientations. In AIDA, et al (Ed). *The Science and Praxis of Complexity*. Tokyo: United Nations University, 1984, 69-80.
- [133] DARLEY, V. Emergent Phenomena and Complexity. *Alife IV*, also available electronically at URL: <http://www.cogs.susx.ac.uk/users/ezequiel/alife-page/complexity.html>, 1994.
- [134] DARLEY, VM; KAUFFMAN, SA (forthcoming). Natural Rationality. In ARTHUR, WB et al. (eds) *The Economy as a Complex Evolving System, Volume II*. Reading MA: Addison-Wesley, forthcoming.
- [135] DAVIS, JS; LEBLANC, RJ. A Study of the Applicability of Complexity Measures. *IEEE Transactions on Software Engineering*, 1989, 14, 1366-1372.
- [136] DAWKINS, R. *The Blind Watchmaker*. London: Penguin, 1986.
- [137] DAWKINS, R. The evolution of evolvability. In C.G.LANGTON (Ed.). *Artificial Life*. Reading, MA: Addison-Wesley, 1989.
- [138] DE LUCA, A. Complexity and Information Theory. In G.LONGO (Ed). *Coding and Complexity*. Berlin: Springer-Verlag, 1975, 207-270.
- [139] DIAMOND, AH; MCKINSEY, JCC. Algebras and their subalgebras. *Bulletin of the American Mathematical Society*, 1947, 53, 959-962.
- [140] DOMOTOR, Z. Measurement: empiricist and realist views. In SAVAGE, CW; EHRLICH, P (eds.). *Philosophical and Foundations Issues in Measurement Theory*, Hillsdale, NJ: Lawrence Erlbaum, 1992, 195-221.
- [141] DRAPER, NR; SMITH, H. *Applied Regression Analysis*. New York: John Wiley, 1981.
- [142] DUNNE, PE. *Complexity of Boolean Networks*. London: Academic Press, 1988.
- [143] DUHEM, P. *The Aim and Structure of Physical Theory*. Translated by WIENER, PP, (1954) Princeton: Princeton University Press, 1914.
- [144] DUSSAUCHOY, RL. Generalized Information theory and the Decomposability of Systems. *International Journal of General Systems*, 1982, 9, 13-36.
- [145] DYKE, C. *The Evolutionary Dynamics of Complex Systems*. New York: OUP, 1988.
- [146] EBELING, W; JIMENEZ-MONTANO, MA. On Grammars, Complexity and Information Measures of Biological Macromolecules. *Mathematical Bioscience*, 1980, 52, 53-71.

- [147] EDMONDS, B. What is Complexity? - The philosophy of complexity per se with application to some examples in evolution, in F. Heylighen & D.Aerts (eds.): *The Evolution of Complexity*, Kluwer, Dordrecht, 1998.
- [148] EDMONDS, B. *Modelling Bounded Rationality using Evolutionary Techniques*. AISB Workshop on Evolutionary Computing, Manchester, 1997. *Lecture Notes in Computer Science*, 1997, 1305, 31-42.
- [149] EDMONDS, B. *From Complexity to Agent Modelling and Back Again - some implications for economics*. Workshop on Economics and the Sciences of Complexity, Namur, Brussels, May 1997.
- [150] EDMONDS, B. *Complexity and Scientific Modelling*. 20th International Wittgenstein Symposium, Kirchberg am Wechsel, Austria, August 1997.
- [151] EDMONDS, B; MOSS, SJ; WALLIS, S. *Logic, Reasoning and a Programming Language for Simulating Economic and Business Processes with Artificial Intelligent Agents*. In EIN-DOR, P. (ed.): *Artificial Intelligence in Economics and Management*. Boston: Kluwer Academic Publishers, 221-230, 1996.
- [152] EDMONDS, B. *Capturing Social Embeddedness: a Constructivist Approach*. *Adaptive Behavior*, forthcoming.
- [153] EHRENFUCHT, A; ZEILGER, P. *Complexity Measures for Regular Expressions*. 6th Annual ACM Symposium on the Theory of Computation, Seattle, WA, 1974, 1974.
- [154] EPSTEIN, RL. *The Semantic Foundations of Logic, Vol. 1: Propositional Logics*. Dordrecht: Kluwer, 1990.
- [155] FELDMAN, JA. *Some decidability results on grammatical inference and complexity*. *Information and Control*, 1972, 20, 244-262.
- [156] FERDINAND, AE. *Complex systems are those that work even with maximum entropy*. *International Journal of General Systems*, 1974, 1, 19-33.
- [157] FLOOD, RL. *Complexity: A definition by construction of a conceptual framework*. *Systems Research*, 1987, 4, 177-185.
- [158] FLOOD, RL; CARSON, ER. *Dealing with Complexity*. New York: Plenum Press, 1988.
- [159] FOSTER, MH; MARTIN, ML (Eds.). *Probability, Confirmation and Simplicity*. New York: Odyssey Press, 1966.
- [160] FRASER, AM. *Measuring Complexity in Terms of Mutual Information*. In ABRAHAM, NB (Ed). *Measures of Complexity and Chaos*. New York: Plenum Press, 1989, 117-119.
- [161] VAN FRASSEN, BC. *The Scientific Image*. Oxford: Clarendon, 1980.
- [162] FREGE, G. *Begriffsschrift*. Halle: Nebert, 1879.

- [163] FUTIA, C. The Complexity of Economic Decision Rules. *Journal of Mathematical Economics*, 1975, 4, 289-299.
- [164] GAINES, BR. On the Complexity of Casual Models. *IEEE Transactions on Systems, Man and Cybernetics*, 1975, 6, 56-59.
- [165] GAINES, BR. System Identification, Approximation and Complexity. *International Journal of General Systems*, 1976, 3, 145-174.
- [166] GALBRAITH, J. *Designing Complex Organisations*. Reading, MA: Addison-Wesley, 1973.
- [167] GALLO, G; LONGO, G; PALLOTTINO, S; et al. Directed Hypergraphs and Applications. *Discrete Applied Mathematics*, 1993, 42, 177-201.
- [168] GELL-MANN, M. *The Quark and the Jaguar - adventures in the simple and the complex*. London: Little, Brown and Co., 1994.
- [169] GELL-MANN, M. What is Complexity? *Complexity*, 1995, 1, 16-19.
- [170] GELL-MANN, M; LLOYD, S. Information Measures, Effective Complexity and Total Information. *Complexity*, 1996, 2, 44-52
- [171] GEORGE, B. Tests for System Complexity. *International Journal of General Systems*, 1977, 3, 253-257.
- [172] GEORGE, DAR. Chaos and Complexity in Economics: Review Article. *Journal of Economic Surveys*, 1990, 4, 397-404.
- [173] GIARINI, O. The Consequences of Complexity in Economics: Vulnerability, Risk, and Rigidity Factors in Supply. In AIDA, et al (Ed). *The Science and Praxis of Complexity*. Tokyo: United Nations University, 1984, 133-145.
- [174] GIBSON, E; SCHUTZE, CT; SALOMON, A. The Relationship Between the Frequency and the Processing Complexity of Linguistic Structure. *Journal of Psycholinguistic Research*, 1996, 25, 59-92.
- [175] GIERE, RN. Constructive Realism. In CHURCHLAND, PM; HOOKER, CW (eds.). *Images of Science*, Chicago: University of Chicago Press, 1985, 75-98.
- [176] GIERE, RN. The Cognitive Structure of Scientific Theories. *Philosophy of Science*, 1994, 61, 276-296.
- [177] GIRARD, JY. Linear Logic. *Theoretical Computer Science*, 1987, 50, 1-102.
- [178] GIRARD, JY. *Proof Theory and Logical Complexity*. Naples: Bibliopolis, 1987.
- [179] GLUCK, R; KLIMOV, A. Reduction of Language Hierarchies. 14th International Congress on Cybernetics, Namur, Belgium, 1995, 1995.

- [180] GÖDEL, K. On the length of proofs. *Ergebnisse eines mathematischen Kolloquiums*, 1936, 7, 23-24.
- [181] GODFREY-SMITH, P. *Complexity and the Function of Mind in Nature*. Cambridge: Cambridge University Press, 1996.
- [182] GOGUEN, JA. Complexity of Hierarchically Organised Systems. *International Journal of General Systems*, 1977, 3(4), 233-251.
- [183] GOLAY, MW; SEONG, PH; MANNO, VP. A Measure of the Difficulty of System Diagnosis and its Relationship to Complexity. *International Journal of General Systems*, 1989, 16, 1-23.
- [184] GOLDMAN, SA; KEARNS, MJ; SCHAPIRE, RE. On the Sample Complexity of Weak Learning. *Information and computation*, 1995, 117, 276.
- [185] GOOD, IJ. Corroboration, Explanation, Evolving Probability and a Sharpened Razor. *British Journal for the Philosophy of Science*, 1969, 19, 123-43.
- [186] GOODMAN, N. *The Structure of Appearance*. Indianapolis: Bobbs-Merrill, 1966.
- [187] GOLDSMITH, RE; NUGENT, N. Innovativeness and Cognitive Complexity, *Psychological Reports*, 1984, 55, 431-438.
- [188] GORODKIN, J; SORENSEN, A; WINTHER, O. Neural Networks and Cellular Automata Complexity. *Complex Systems*, 1993, 7, 1-23.
- [189] GOTTINGER, HW. Complexity and Information Technology in Dynamic Systems. *Kybernetes*, 1975, 4, 129-141.
- [190] GOTTINGER, HW. Complexity and Dynamics: Applications of Dynamic Systems Theory. *IEEE Transactions on Systems, Man and Cybernetics*, 1976, 6, 867-873.
- [191] GOTTINGER, HW. Choice and Complexity. *Mathematical Social Sciences*, 1987, 14, 1-17.
- [192] GOTTINGER, HW; LEINFELLNER, W (Eds.). *Decision Theory and Social Ethics: Issues in Social Choice*. Dordrecht: Reidel, 1978.
- [193] GRASSBERGER, P. Towards a quantitative theory of self-generated complexity. *International Journal of Theoretical Physics*, 1986, 25(9), 907-938.
- [194] GRASSBERGER, P. Problems in Quantifying Self-organized complexity. *Helvetica Physica Acta*, 1989, 62, 498-511.
- [195] GRASSBERGER, P. Information and Complexity Measures in Dynamical Systems. In ATMANSPACHER, H; SCHEINGRABER, H (Eds). *Information Dynamics*. New York: Plenum Press, 1991, 15-33.

- [196] GREEN, DG. Syntactic modelling and simulation. *Simulation*, 1990, 54, 281-286.
- [197] GREEN, DG. Emergent Behaviour in Biological Systems. In GREEN, DG; BOSSOMAIER, TJ (Eds). *Complex Systems - From Biology to Computation*. Amsterdam: OS Press, 1993, 24-35.
- [198] GREENBERG, WJ. A Theory of Complexes. Preprint, department of English, college of humanities, University of Puerto Rico at Rio Piedras, 1990.
- [199] GROENEWOLD, H. J. The model in physics. *Synthese*, 1960, 12, 222-227.
- [200] GRUNBERG, E. "Complexity" and "Open Systems" in Economic Discourse. *Journal of Economic Issues*, 1978, 12, 541-560.
- [201] GUNSTEREN, W. F; BERENDSEN, H. J. C. *Computational Simulation of Molecular Dynamics: Methodology, Applications and Perspectives in Chemistry*. *Angewandte Chemie – International Edition in English*, 1990, 29, 992-1023.
- [202] GUNTHER, R; SHAPIRO, B; WAGNER, P. Complex Systems, complexity measures, grammars and model inferring. *Chaos, Solitons and Fractals*, 1994, 4, 635-651.
- [203] GUSEV, VD; KULICHKOV, VA; CHUPKHINA, OM. Genome Complexity Analysis 1: Complexity Measures and the Classification of Structural Features. *Molecular Biology*, 1991, 25, 669-677.
- [204] HAGESETH, JA. Relationships among cognitive complexity variables, *Psychological Reports*, 1983, 52, 473-474.
- [205] HAKEN, H. *Information and Self-Organisation: a macroscopic approach to complex systems*. Berlin: Springer-Verlag, 1988. Springer Series in Synergetics.
- [206] HALSTEAD, MH. *Elements of Software Science*. New York: Elsevier, 1977.
- [207] HARNAD, S. The symbol grounding problem. *Physica D*, 1981, 42, 335-346.
- [208] HARTMAN, S. *Modelling and the Aims of Science*. 20th International Wittgenstein Symposium, Kirchberg am Wechsel, 1997.
- [209] HAWRNACK, J; ZYGMUNT, J. On the Degree of Complexity of Sentential Logics. *Studia Logica*, 1981, 4, 142-153.
- [210] HAYEK, FA. The Theory of Complex Phenomena. In BUNGE, M (Ed). *The Critical Approach to Science and Philosophy*. London: Collier McMillan, 1964, 332-349.
- [211] HEMMERLING, A. On Genuine Complexity and Kinds of Nondeterminism. *Journal of information processing and cybernetics*, 1995, 30, 77.
- [212] HEMPEL, C. G. *Aspects of Scientific Explanation*. New York: Free Press, 1965.

- [213] HEMPEL, CG; OPPENHEIM, P. Studies in the Logic of Explanation. *Philosophy of Science*, 1948, 15, 135-175.
- [214] HENRY, S; KAFURA, K. Software Structure Metrics based on Information Flow. *IEEE Transactions on Software Engineering*, 1981, 7(5), 510-518.
- [215] HERROELEN, W; VANGLIS, A. On the use of Flow Dominance in Complexity Measures for Facility Layout Problems. *International Journal of Production Research*, 1985, 23, 97-108.
- [216] HESSE, MB. *Models and Analogies in Science*. London: Sheed and Ward, 1963.
- [217] HESSE, MB. Simplicity. In EDWARDS, P (Ed). *Encyclopedia of Philosophy*. New York: Macmillan, 1967, 445-449.
- [218] HEYLIGHEN, F. Relational Closure: a Mathematical Concept for Distinction-making and complexity analysis. In TRAPPL, R (Ed). *Cybernetics and Systems '90*. Singapore: World Scientific, 1990, 335-341.
- [219] HEYLIGHEN, F. Modelling Emergence. ftp papers from Principia Cybernetica server, also for "world Futures: the Journal of General Evolution", special issue on creative evolution, G. Kampis (ed), 1991.
- [220] HEYLIGHEN, F. Self-Organization, Emergence and the Architecture of Complexity. In *Proceedings of the European Congress on System Science*. Paris: AFCET, 1992, 23-32.
- [221] HEYLIGHEN, F. The Growth of Structural and Functional Complexity during Evolution. In HEYLIGHEN, F & AERTS, D (eds.) *The Evolution of Complexity*. Amsterdam: Kluwer Academic Publishers, 1996.
- [222] HILBERT, D.; BERNAYS, P. *Grundlagen der Mathematik*, Vol. 1. Berlin: Springer, 1934.
- [223] HINEGARDNER, R; ENGELBERG, J. Biological Complexity. *Journal of Theoretical Biology*, 1983, 104, 7-20.
- [224] HITCHCOCK, D. Relevance. *Argumentation*, 1992, 6, 251-270.
- [225] HO, JKK; SCULLI, D. System Complexity and the Design of Decision Support Systems. *Systems Practice*, 1995, 8, 505-516.
- [226] HOGG, T; HUBERMAN, BA. Order, Complexity and Disorder. *Mondes en Developpement*, 1986, 54-55.
- [227] HOGG, T; HUBERMAN, BA; JACQUELINE, MM. The stability of ecosystems. *Proceedings of the Royal Society of London B*, 1989, 237, 43-51.
- [228] HOLLAND, J. *Adaption in Natural and Artificial Systems*. Ann Arbor, Michigan: University of Michigan Press, 1975.

- [229] HOLM, HJ. Complexity in Economic Theory. Lund, Sweden: University of Lund: Lund Economic Studies, 1993.
- [230] HOOKER, JN; VINAY, V. Branching Rules for Satisfiability. Carnegie Mellon University, Graduate School of Industrial Administration working paper WP 1994-09, 1994.
- [231] HOPCROFT, JE; ULLMAN, JD. Introduction to Automata Theory, Languages, and Computation. Reading, Massachusetts: Addison-Wesley, 1979.
- [232] HOPS, JM; SHERIF, JS. Development and application of composite complexity models and a relative complexity metric in a software maintenance environment. Journal of Systems and Software, 1995, 31, 157-169.
- [233] HORGAN, J. From Complexity to Perplexity. Scientific American, 1995, 272, 74-79.
- [234] HOWATT, JW; BAKER, AL. Rigorous Definition and Analysis of Program Complexity Measures - An example using nesting. Journal of Systems and Software, 1989, 10, 139-150.
- [235] HROMKOVIC, J; KARI, J; KARI, L. Some Hierarchies for the Communication Complexity Measures of Cooperating Grammar Systems. Theoretical Computer Science, 1994, 127, 123-147.
- [236] HUGHES, R. G. Models and Representation. Philosophy of Science, 1997, 64(proc), S325-S336.
- [237] HUBERMAN, BA; HOGG, T. Complexity and Adaption. Physica D, 1986, 22, 376-384.
- [238] ITAI, A; MAKOWSKY, JA. Unification as a Complexity Measure for Logic Programming. Journal of Logic Programming, 1987, 4, 105-117.
- [239] JACKO, JA; SALVENDY, G. Hierarchical menu design: breadth, depth and task complexity. Perceptual and Motor Skills, 1996, 82, 1187-1202.
- [240] JASKOWSKI, S. Trois Contributions au Calcul des Propositions Bivalentes. Studia Societatis Scientiarum Torunensis, 1948, 1(1), 1-15.
- [241] JEFFREYS, H. Scientific Inference. Cambridge: Cambridge University Press, 1937.
- [242] JOHNSON, J. A Theory of Stars in complex Systems. In CASTI, JL; KARLQUIST, A (Eds). Complexity Language and Life: Mathematical Approaches. Berlin: Springer-Verlag, 1986, 21-61.
- [243] KAMPIS, G. Information, Computation and Complexity. In CARVALLO, ME (Ed). Nature, Cognition and Systems. Dordrecht: Kluwer, 1988, 313-320.
- [244] KAMPIS, G. Self-Modifying Systems in Biology and Cognitive Science: A New Framework for Dynamics, Information and Complexity. Oxford: Pergamon Press, 1991.

- [245] KAMPIS, G; CSANYI, V. Simple Models Do Not Eliminate Complexity from the Real World. *Journal of Theoretical Biology*, 1985, 115, 467-469.
- [246] KAMPIS, G; CSANYI, V. Notes on Order and Complexity. *Journal of Theoretical Biology*, 1987, 124, 111-121.
- [247] KANEKO, K; TSUDA, I. Constructive Complexity and Artificial Reality: An Introduction. *Physica D*, 1994, 75, 1-10.
- [248] KAPLOW, L. A Model of the Optimal Complexity of Rules. National Bureau of Economic Research Working paper No. 3958, 1992.
- [249] KAUFFMAN, SA. *The Origins of Order*. New York: Oxford University Press, 1993.
- [250] KELLY, GA. *The Psychology of Personal Constructs*, New York: Norton, 1955.
- [251] KELLY, JS. Social Choice and Computational Complexity. *Journal of Mathematical Economics*, 1988, 17, 1-8.
- [252] KELMANS, AK. A Comparison of Graphs by their number of spanning trees. *Discrete Mathematics*, 1976, 16, 241-261.
- [253] KEMENY, JG. The Use of Simplicity in Induction. *The Philosophical Review*, 1953, 62, 391-408.
- [254] KEMENY, JG. Two Measures of Complexity. *The Journal of Philosophy*, 1953, 52, 722-733.
- [255] KEMENY, JG. A New Approach to Semantics, Part I. *Journal of Symbolic Logic*, 1956.
- [256] KEMPER, S; RICE, K; CHEN, Y. Complexity metrics and growth curves for measuring grammatical development from five to ten. *First Language*, 1995, 15, 151-166.
- [257] KHALIL, EL. Organizations, Naturalism and Complexity. *Review of Social Economy*, 1995, 53, 393-419.
- [258] KIMELMAN, D; LEBAN, B. Reduction of Visual Complexity in Dynamic Graphs. *DIMACS Graph Drawing'94*, 1994.
- [259] KINDLMANN, P. Stability v. Complexity in Model Computational Communities. *Lecture Notes in BioMathematics*, 1984, 54, 191-207.
- [260] KINGSNORTH, A. Complexities of Complexity. *Bulletin of the American Schools of Oriental Research*, 1993, 292, 107-120.
- [261] KINNEAR, KE (ed.). *Advances in Genetic Programming*. Cambridge, MA: MIT Press, 1994.

- [262] KLIR, GJ. The Many Faces of Complexity. In AIDA, et al (Ed). The Science and Praxis of Complexity. Tokyo: United Nations University, 1984, 81-98.
- [263] KLIR, GJ. Architecture of Systems Problem Solving. New York: Plenum Press, 1985.
- [264] KLIR, GJ. Complexity: Some General Observations. Systems Research, 1985, 2, 131-140.
- [265] KLIR, GJ; FOLGER, TA. Fuzzy Sets, Uncertainty and Information. New Jersey: Prentice Hall, 1988.
- [266] KOLMOGOROV, AN. Three Approaches to the quantitative definition of Information. Problems of Information Transmission, 1965, 1, 1-17.
- [267] KOLMOGOROV, AN; TICHOMIROV, WM. e-Entropie und e-Kapazität von Mengen in Funktionalräumen. In Arbeiten zur Informationstheorie. Berlin: VEB Deutscher Verlag der Wissenschaften, 1960.
- [268] KOPPEL, M. Complexity, Depth and Sophistication. Complex Systems, 1987, 1, 1087-1091.
- [269] KOPPEL, M. Structure. In HERKEN, R (Ed). The Universal Turing Machine, A Half Century Survey. Oxford: Oxford University Press, 1988, 435-452.
- [270] KOZA, JR. Genetic Programming: On the Programming of Computers by Natural Selection. Cambridge, MA: MIT Press, 1992.
- [271] KRANTZ, D; LUCE, D; SUPPES, P; TVERSKY, A. Foundations of Measurement, Vol.1. New York: Academic Press, 1971.
- [272] KROHN, K; RHODES, JL. Complexity of Finite Semi-Groups. Annals of Mathematics, 1968, 88, 128-160.
- [273] KROLL, NEA; KLIMESCH, W. Semantic Memory - Complexity or Connectivity. Memory and Cognition, 1992, 20, 192-210.
- [274] KUHN, TS. The Structure of Scientific Revolutions. Chicago: Chicago University Press, 1962.
- [275] KUHN, TS. Some Thoughts on Paradigms. In SUPPE, F (ed.). The Structure of Scientific Theories. Urbana, IL: University of Urbana Press, 1973, 459-482.
- [276] KYBURG, HE. Measuring Errors of Measurement. In SAVAGE, C. W; EHRLICH, P (eds.). Philosophical and Foundations Issues in Measurement Theory, Hillsdale, NJ: Lawrence Erlbaum, 1992, 75-91.
- [277] LAKSHMANAN, KB; JAYAPRAKASH, S; SINHA, PK. Properties of Control-Flow Complexity Measures. IEEE Transactions on Software Engineering, 1991, 17, 1289-1295.

- [278] LAZAREV, VI. Complexity and Synthesis of Minimal Logic Circuits using Multiplexers. *Cybernetics*, 1992, 28, 796-799.
- [279] LEMPEL, A; ZIV, J. On the complexity of finite sequences. *IEEE Transactions on Information Theory*, 1976, 22, 75-81.
- [280] LESTEL, D. The metaphors of complexity: the language and cognitive resources of artificial life. *Social Science Information*, 1996, 35, 511-540.
- [281] LEVESQUE, HJ. Logic and the Complexity of Reasoning. *Journal of Philosophical Logic*, 1989, 17, 355-389.
- [282] LEVINE, RD; TRIBUS, M (Eds.). *The Maximum Entropy Principle*. Cambridge, Massachusetts: MIT Press, 1979.
- [283] LEVINS, RD. The Limits of Complexity. In PATTEE, HH (Ed). *Hierarchy Theory – The Challenge of Complex Systems*. New York: George Braziller, 1973, 109-127.
- [284] LI, M; VITANYI, JMB. Statistical Properties of Finite Sequences with High Kolmogorov Complexity. *Mathematical Systems Theory*, 1994, 27, 365-376.
- [285] LI, M; VITANYI, PMB. Philosophical Issues in Kolmogorov Complexity. *Lecture Notes in Computer Science*, 1992, 623, 1-15.
- [286] LI, M; VITANYI, PMB. *An Introduction to Kolmogorov Complexity and Its Applications*. New York: Springer-Verlag, 1993.
- [287] LI, W. On the Relationship between Complexity and Entropy for markov Chains and Regular Languages. *Complex Systems*, 1991, 5, 381-399.
- [288] LIGGGESMEYER, P. A set of complexity metrics for guiding the software test process. *Software Quality Journal*, 1995, 4, 257-273.
- [289] LINDGREN, K; NORDAHL, MG. Complexity measures and cellular automata. *Complex Systems*, 1988, 2, 409.
- [290] LIPMAN, BL; SRIVASTAVA, S. Informational Requirements and Strategic Complexity in Repeated Games. *Games and Economic Behaviour*, 1990, 2, 273-290.
- [291] LLOYD, S. Physical Measures of Complexity. In JEN, E (Ed). *1989 Lectures in Complex Systems*. Redwood City, California: Addison-Wesley, 1990, 67-73.
- [292] LLOYD, S; PAGELS. Complexity as Thermodynamic Depth. *Annals of Physics*, 1988, 188, 186-213.
- [293] LÖFGREN, L. Complexity of Descriptions of Systems: A foundational Study. *International Journal of General Systems*, 1974, 3, 197-214.

- [294] LÖFGREN, L. Syntactic and Semantic reduction of Theories. *Journal for Symbolic Logic*, 1976, 41, 268-269.
- [295] LÖFGREN, L. Complexity of Systems. In SINGH, M (Ed). *Systems and Control Encyclopedia*. Oxford: Pergamon, 1987, 704-709.
- [296] LOPEZ, LR; CAUFIELD, LJ. A Principle of Minimum Complexity in Evolution. *Lecture Notes in Computer Science*, 1991, 496, 405-409.
- [297] LÓPEZ-RUIZ, R; MANCINI, HL; CALBERT, X. A statistical measure of complexity. *Physics Letters A*, 1995, 209, 321-326.
- [298] LUGOSI, G; ZEGER, K. Concept Learning Using Complexity Regularization. *IEEE Transactions on Information Theory*, 1996, 42, 48-54.
- [299] LUHMANN, N. Complexity and Meaning. In AIDA ET AL. (Ed). *The Science and Praxis of Complexity*. Tokyo: United Nations University, 1985, 99-104.
- [300] LUKASIEWICZ, J. The Shortest Axiom of the Implicational Calculus of Propositions. *Proceedings of the Royal Irish Academy*, 1948, 52, 25-33.
- [301] LUPTON, P. Simplicity and Misrepresentation. Available electronically at URL: <http://cogsci.l.chiba-u.ac.jp/IPPE/PhilofMind/Lupton.SimplicityandMisrepresentation/index.html>, 1994.
- [302] LYON, ML. Complexity and Emergence: The seduction and reduction of non-linear models in the social sciences. *Complex Systems* 92, Australia National University, 1992.
- [303] MACHLIN, R. The Complex Behaviour of Simple Machines. *Physica D*, 1990, 42, 85-98.
- [304] MADDOX, J. Complicated Measures of Complexity. *Nature*, 1990, 344, 705.
- [305] MAKINEN, E. 2 Complexity Measures for Context-free Languages. *International Journal of Computer Mathematics*, 1988, 1, 29-34.
- [306] MAKLAD, MS; NICHOLS, ST. A New Approach to Model Structure Discrimination. *IEEE Transactions on Systems, Man and Cybernetics*, 1980, 10, 78-84.
- [307] MARCUS, MJ. The Theory of Connecting Networks and their Complexity: A Review. *Proceedings of the IEEE*, 1977, 65, 1263-1271.
- [308] MARGALEF, R. Ecosystems: Diversity and Connectivity as measurable components of their complication. In AIDA, et al (Ed). *The Science and Praxis of Complexity*. Tokyo: United Nations University, 1984, 228-244.
- [309] MARTIN-LOF, P. The Definition of Random Sequences. *Information and Control*, 1966, 9, 602-619.

- [310] MARTINEZ, JL. On Complexity and Simplicity as Different Evolutionary Strategies. *Evolutionary Theory*, 1995, 10, 317-320
- [311] MASUCH, M; HUANG, Z. A logical deconstruction of organizational action: formalising J.D. Thompson's 'Organisations in Action' in a multi-agent action logic. CCSOM working paper 94-120, Department of Statistics and Methodology, University of Amsterdam, 1994.
- [312] MATA-TOLEDO, RA; GUSTAFSON, DA. A Factor Analysis of Software Complexity Measures. *Journal of Systems and Software*, 1992, 17, 267-273.
- [313] MCCABE. A Complexity Measure. *IEEE Transactions on Software Engineering*, 1976, 2, 308-320.
- [314] MCINTYRE, LC. Complexity and Social Scientific Laws. *Synthese*, 1993, 97, 209-227.
- [315] MCMULLEN, C; SHEARER, J. Prime Implicants, Minimum Cover and the Complexity of Logic Simplification. *IEEE Transactions on Computers*, 1986, 35, 761-762.
- [316] MCSHEA, D. Complexity and Evolution: what everybody knows. *Biology and Philosophy*, 1991, 6(3), 303-3024.
- [317] MCSHEA, D. Meatzoan Complexity and Evolution: is there a trend? *Evolution*, 1996, 50, 477-492
- [318] MEER, K. On the Relations Between Discrete and Continuous Complexity Theory. *Mathematical Logic Quarterly*, 1995, 41, 281-286.
- [319] MEINEL, C. Logic vs. Complexity Theoretic Properties of the Graph Accessibility Problem for Directed Graphs of Bounded Degree. *Information Processing Letters*, 1990, 34, 143-146.
- [320] MEREDITH, CA. On an Extended System of the Propositional Calculus. *Proceedings of the Royal Irish Academy*, 54.
- [321] MEREDITH, CA. Single Axioms for the Systems (C, N), (C, O) and (A, N) of the Two-valued Propositional Calculus. *The Journal of Computing Systems*, 1, paper 10.
- [322] MEYER, AR; RITCHIE, DM. The Complexity of Loop Programs. In *Proceedings of the 22nd National Conference*. Washington DC: Thompson Book Company, 1967, 465-469.
- [323] MIKULECKY, DC. Life, Complexity and the Edge of Chaos: Cognitive Aspects of Communication between cells and other components of living systems. Available electronically at URL: <http://griffin.vcu.edu/complex/mikulecky/rev.htm>, 1995.
- [324] MILLER, DA; ZUCKER, SW. Complexity and Optimality - A Commentary. *Behavioural and Brain Sciences*, 1991, 14, 227.
- [325] MILLER, GA. The magical number seven, plus or minus two: Some limits on our capacity for processing information. *Psychological Review*, 1956, 63, 81-97.

- [326] MILLER, GA; CHOMSKY, N. Finitary models of language users. In LUCE, RD; BUSH, RR; GALANTER, E (Eds). Handbook of Mathematical Psychology. New York: Wiley, 1963, 419-491.
- [327] MITCHELL, S. D. Pragmatic Laws. Philosophy of Science, 1997, 64(proc), S468-S479.
- [328] MORGAN, M. S. The Technology of Analogical Models. Philosophy of Science, 1996, 64(proc), S304-S314.
- [329] MORGAN, M; MORRISON, M (eds.). Models as Mediators. Cambridge: CUP, forthcoming.
- [330] MORIN, E. Complexity. International Journal of Social Science, 1974, 26, 583-597.
- [331] MORIN, E. On the Definition of Complexity. In AIDA, EA (Ed). The Science and Praxis of Complexity. Tokyo: United Nations University, 1984, 62-68.
- [332] MOSHOWITZ, A. Entropy and the Complexity of Graphs. Bulletin of Mathematical Biophysics, 1968, 30, 175-204,225-40.
- [333] MOSS, S; EDMONDS, B. Modelling Economic Learning as Modelling, Cybernetics and Systems, 1998, 29, 5-37.
- [334] MOSS, S; EDMONDS, B; GAYLARD, H. Modelling R&D Strategy as a Network Search Problem. Workshop on the Multiple Linkages between Technological Change, Human Capital and the Economy, University 'Tor Vergata' of Rome, March 1996.
- [335] MULHAUSER, GR. To Simulate or Not to Simulate: A Problem of Minimising Functional Logical Depth. Lecture Notes in Artificial Intelligence, 1995, 929, 530-543.
- [336] MURPHY, PM; PAZZANO, MJ. Exploring the Decision Forest: An Empirical Investigation of Occam's Razor in Decision Tree Induction. Journal of Artificial Intelligence Research, 1994, 1, 257-275.
- [337] NAGEL, E. The Structure of Science. New York: Harcourt Brace, 1961.
- [338] NAYLOR, AW. On Decomposition Theory: Generalised Dependence. IEEE Transactions on Systems, Man and Cybernetics, 1981, 10, 699-713.
- [339] NELSON, RJ. Structure of Complex Systems. Philosophy of Science Association, 1976, 2, 523-542.
- [340] NIELSEN, ME. H-Comp: a program to calculate information complexity. Behaviour Research Methods, Instruments and Computers, 1996, 28, 483-485.
- [341] O'NEAL, MB; EDWARDS, WR. Complexity Measures for Rule-Based Programs. IEEE Transactions on Knowledge and Data Engineering, 1994, 6, 669-680.

- [342] O'NEILL, RV; DEANGELIS, DL; WAIDE, JB; et al. A Hierarchical Concept of Ecosystems. Princeton, NJ: Princeton University Press, 1986.
- [343] OSHERSON, DN; WEINSTEIN, S. On Advancing Simple Hypothesis. *Philosophy of Science*. 1990, 57, 266-277.
- [344] PAKKAN, M; AKMAN, V. Issues in Common Sense Set-theory. *Artificial Intelligence Review*, 1994, 8(4), 279-308.
- [345] PAPENTIN, F. On Order and Complexity. *Journal of Theoretical Biology*, 1980, 87, 1-456.
- [346] PATTEE, H (Ed.). *Hierarchy Theory, the Challenge of Complex Systems*. New York: Braziller, 1973.
- [347] PATTEE, H. Dynamic and Linguistic Modes of Complex Systems. *International Journal of General Systems*, 1977, 3, 259-266.
- [348] PATTEE, H. Evolving self-reference: matter, symbols and semantic closure. *Communication and Cognition - Artificial Intelligence*, 1995, 12, 9-27.
- [349] PEARL, J. On the Connection Between the Complexity and Credibility of Inferred Models. *International Journal of General Systems*, 1978, 4, 255-264.
- [350] PELITI, L; VULPIANI, A (Eds.). *Measures of Complexity*. Berlin: Springer-Verlag, 1988.
- [351] PERLIS, A; SAYWARD, F; SHAW, M (Eds.). *Software Metrics*. Cambridge (MA): MIT Press, 1981.
- [352] PHILLIPS, W and T, S. *Systems Thinking and the Quality of Life*. Proceedings of the Society for General Systems Research Annual Meeting, 1975.
- [353] PIMM, S. The complexity and stability of ecosystems. *Nature*, 1984, 307, 321-326.
- [354] PINCUS, S. Approximate entropy (ApEn) as a complexity measure. *Chaos*, 1995, 5, 110-117.
- [355] PIPPENGER, N. Complexity Theory. *Scientific American*, 1978, 239, 90-100.
- [356] PIPPENGER, N. Invariance of Complexity Measures for Networks with Unreliable Gates. *Journal of the Association of Computing Machinery*, 1989, 36, 531-539.
- [357] POON, L; GREBOGI, C. Controlling Complexity. *Physical Review Letters*, 1995, 75, 4023-4026.
- [358] POPPER, KR. *Logic of Scientific Discovery*. London: Hutchinson, 1968.
- [359] PRATHER, RE. An axiomatic theory of software complexity research. *The Computer Journal*, 1984, 27, 340-346.

- [360] PRIBRAM, KH. Complexity and Causality. In AIDA, S, et al (Ed). The Science and Praxis of Complexity. Tokyo: United Nations University, 1984, 119-132.
- [361] PRIGOGINE, I; STENGERS, I. Order out of Chaos - Man's new dialogue with nature. Toronto: Bantam Books, 1984.
- [362] PRIOR, AN. Formal Logic. London: Oxford University Press, 1962.
- [363] PUTNAM, H. What Theories are Not. In NAGEL, E; SUPPES, P; TARSKI, A (eds.). Logic Methodology and the Philosophy of Science: Proceedings of the 1960 International Congress. Stanford, CA: Stanford University Press, 1962, 240-251.
- [364] QUINE, WVO. Simple Theories of a Complex World. In The Ways of Paradox. New York: Random House, 1960, 242-246.
- [365] RACCOON, LBS. The Complexity Gap. Software Engineering Notes, 1995, 20, 37-44.
- [366] RAM, AL. A Study of Cognitive Complexity among College Students. Journal of Psychological Researches, 28, 84-90
- [367] RAMAMOORTHY, CV. An analysis of graphs by connectivity considerations. Journal of the Association of Computing Machinery, 1966, 13, 211-222.
- [368] RAMIREZ, DE. On 2 Nonequivalent Measures of Complexity. IEEE Transactions on Systems, Man and Cybernetics, 1989, 19, 1073-1077.
- [369] RAMSEY, FP. The foundations of mathematics. London: Routledge & Kegan Paul, 1950. [original 1929]
- [370] RAY, TS. Evolution and Complexity. In COWAN, G; PINES, D; MELTZER, D (Eds). Complexity: Metaphors, Models and Reality. REading, MA: Addison-Wesley, 1994, 161-173.
- [371] RAY, TS. Evolution, Complexity, Entropy and Artificial Reality. Physica D, 1994, 75, 239-263.
- [372] REDHEAD, M. 1980 Models in Physics. British Journal for the Philosophy of Science, 31:145-163.
- [373] REGGIANI, A; NIJKAMP, P. Competition and complexity in spatially connected networks. System dynamics review, 1995, 11, 51-66.
- [374] REINBERGER, H-J. Experimental Complexity in Biology: Some Epistemological and Historical Remarks. Philosophy of Science, 1997, 64(proc), S245-S254.
- [375] DE REYCK, B; HERROELEN, W. On the use of the complexity index as a measure of complexity in activity networks. European Journal of Operational Research, 1996, 91, 347-366.
- [376] RICHMOND, SA. A Simplification of the Theory of Simplicity. Synthese, 1996, 107, 373-393.

- [377] RISSANEN, J. Modelling by the shortest data description. *Automatica*, 1978, 14, 465-471.
- [378] RISSANEN, J. Stochastic Complexity and the MDL Principle. *Econometric Reviews*, 1987, 6, 85-102.
- [379] RISSANEN, J. Complexity of Models. In ZUREK, WH (Ed). *Complexity, Entropy and the Physics of Information*. Redwood City, California: Addison-Wesley, 1990, 117-125.
- [380] ROBINSON, TT. Independence of Two Nice Sets of Axioms for the Propositional Calculus. *Journal for Symbolic Logic*, 1968, 33, 265-270.
- [381] ROBERTS, FS. *Measurement Theory: with applications to decision making, utility and the social sciences*. Reading, MA: Addison-Wesley, 1979.
- [382] ROCK, RA. Integrative Complexity and non-specific set as determinants of performance in a complex solving task. *Journal of Behavioural Science*, 1968, 1, 17-25.
- [383] ROSEN, BK. Syntactic Complexity. *Information and Control*, 1974, 24, 305-335.
- [384] ROSEN, R. Complexity and system descriptions. In HARNETT, WE (Ed). *Systems: Approaches, theories, Applications*. Dordrecht, Holland: D.Reidel, 1977, 169-175.
- [385] ROSEN, R. *Anticipatory Systems*. New York: Pergamon, 1985.
- [386] ROSEN, R. On Information and Complexity. In CASTI, JL; KARLQUIST, A (Eds). *Complexity, Language and Life: Mathematical Approaches*. Berlin: Springer, 1985, 174-195.
- [387] ROSEN, R. Organisms as Causal Systems Which Are Not Mechanisms: An Essay into the Nature of Complexity. In ROSEN, R (Ed). *Theoretical Biology and Complexity: Three Essays on the Natural Philosophy of Complex Systems*. London: Academic Press, 1985, 165-203.
- [388] ROSEN, R. *Life Itself - A Comprehensive Enquiry into the Nature, Origin and Fabrication of Life*. New York: Columbia University Press, 1991.
- [389] ROSEN, R. Bionics Revisited. In HAKEN, H; KARLQUIST, A; SVEDIN, U (Eds). *The Machine as Metaphor and Tool*. Berlin: Springer-Verlag, 1993, 87-100.
- [390] ROSENKRANTZ, RD. *Inference, Method and Decision*. Boston: Reidel, 1976.
- [391] ROTMAN, B. *Taking God out of mathematics and putting the body back*. Stanford, CA: Stanford University Press, 1993
- [392] ROUSE, WB; ROUSE, SH. Measures of Complexity of Fault Diagnosis Tasks. *IEEE Transactions on Systems, Man and Cybernetics*, 1979, 9, 720-727.
- [393] RUSSELL, S; SUBRAMANIAN, D. Mutual constraints on Representation and Inference. In *Machine Learning, Meta-Reasoning and Logics*, BRAZDIL, PB; KONOLIGE, K. (eds.), Boston, MA: Kluwer Academic, 1990, 85-106.

- [394] RUTHEN, R. Adapting to Complexity. *Scientific American*, 1993, 268, 130-135.
- [395] SAHAL, D. Elements of an Emerging theory of Complexity Per Se. *Cybernetica*, 1976, 19, 5-38.
- [396] SAHAL, D. System Complexity: Its Conceptions and Measurement in the Design of Engineering Systems. *IEEE Transactions on Systems, Man and Cybernetics*, 1976, 6, 440-445.
- [397] SAMBROOK, T; WHITEN, A. On the Nature of Complexity in Cognitive and Behavioural Science. *Theory and Psychology*, 1977, 7, 191-213
- [398] SANDERSON, WC. Predictability, Complexity and Catastrophe in a Collapsible Model of Population, Development, and Environmental Interactions. *International Institute for Applied Systems Analysis*, 1994.
- [399] SAUNDERS, PT; HO, MW. On the Increase in Complexity in Evolution. *Journal of Theoretical Biology*, 1981, 90, 515-530.
- [400] SAVAGE, JE. *Complexity of Computing*, 1976.
- [401] SCHAFFER, C. Overfitting Avoidance as Bias. *Machine Learning*, 1993, 10, 153-178.
- [402] SCHAFFER, EF. *Discovery and Explanation in Biology and Medicine*. Chicago: Chicago University Press, 1993.
- [403] SCHRUBEN, L; YCESAN, E. Complexity of simulation models: a graph theoretic approach. In EVANS, GW; MOLLAGHASEMI, M; RUSSELL, EC; et al. (Eds). *Proceedings of the 1993 Winter Simulation Conference*. Piscataway, NJ: IEEE, 1993, 641-649.
- [404] SEAMAN, JM; KOENIG, F. A Comparison Measures of Cognitive Complexity. *Sociometry*, 1974, 37, 375-390.
- [405] SEELEY, D; RONALD, S. The Emergence of Connectivity and Fractal Time in the Evolution of Random Digraphs. *Complex Systems 92*, Australia National University, 1992.
- [406] SELLARS, W. *Philosophical Perspectives*. Reseda, CA: Ridgeway Press, 1977.
- [407] SERRA, R. Some Remarks on Different Measures of Complexity for the Design of Self-organising Systems. In TRAPPL, R (Ed). *Cybernetics and Systems '88*. Dordrecht: Kluwer Academic, 1988, 141-148.
- [408] SHANNON, CE; WEAVER, W. *The Mathematical Theory of Communication*. Urbana, Illinois: University of Illinois Press, 1949.
- [409] SHUQIANG, Z. Cognitive Complexity and Written Production in English as a Second Language. *Language Learning*, 1987, 37, 469-481.
- [410] SIEGELMANN, HT. Computation Beyond the Turing Limit. *Science*, 1995, 268, 545-548.

- [411] SIMON, HA. The Organization of Complex Systems. In PATTEE, HH (Ed). Hierarchy Theory - The challenge of Complex Systems. New York: George Braziller, 1973, 1-27.
- [412] SIMON, HA. How Complex are Complex Systems? Philosophy of Science Association, 1976, 2, 507-522.
- [413] SIMON, HA. Complexity and the Representation of Patterned Sequences of Symbols. In SIMON, HA (Ed). Models of Thought. New Haven, Connecticut: Yale University Press, 1979, 292-306.
- [414] SIMON, HA. The Architecture of Complexity. In The Sciences of the Artificial. Cambridge, Massachusetts: MIT Press, 1981, 192-229.
- [415] SIMON, HA. Economics, Bounded Rationality and the Cognitive Revolution. Brookfield, Vermont: Edward Elgar, 1992.
- [416] SMITH, SW et al. Cognitive Complexity and Gifted Education, 1983.
- [417] SNEED, J. The Logical Structure of Mathematical Physics. Dordrecht: Reidel, 1971.
- [418] SOBER, E. Simplicity. Oxford: Clarendon Press, 1975.
- [419] SOLOMONOFF, RJ. A Formal theory of Inductive Inference. Information and Control, 1964, 7, 1-22, 224-54.
- [420] SOLOMONOFF, RJ. Complexity-based induction systems: comparisons and convergence theorems. IEEE Transactions on Information Theory, 1978, 24, 422-432.
- [421] STEEL, M. The Complexity of Reconstructing Trees from Qualitative Characters and Subtrees. Journal of Classification, 1992, 1992, 91-116.
- [422] STEIN, D. Lectures in the Sciences of Complexity. Redwood City, California: Addison-Wesley, 1989.
- [423] STEVENS, SS. On the Theory of Scales of Measurement. Science, 1946, 103, 677-680.
- [424] STRASSEN, V. Gaussian elimination is not optimal. Numerische Mathematik, 1969, 13, 354-356.
- [425] SUBRAMANIAN, A. The Parallel Complexity of Propagation in Boolean Circuits. Information and computation, 1995, 117, 266.
- [426] SUEDFIELD, P; TETLOCK, PE; STREUFERT, S. Conceptual/Integrative Complexity. In SMITH, PS; ATKINSON, JW; MCCLELLAND, DC; et al. (Eds). Motivation and Personality: Handbook of Thematic Content Analysis. New York: CUP, 1992, 726.
- [427] SUPPE, F. The Search for Philosophical Understanding of Scientific Theories. Suppe, F (ed.). The Structure of Scientific Theories. Urbana, IL: University of Urbana Press, 1973, 3-243.

- [428] SUPPE, F. Exemplars, Theories and Disciplinary Matrixes. SUPPE, F (ed.). The Structure of Scientific Theories. Urbana, IL: University of Urbana Press, 1973, 483-499.
- [429] SUPPE, F. The Semantic Conception of Theories and Scientific Realism. Urbana, IL: University of Urbana Press, 1989.
- [430] SUPPES, P. Introduction to Logic. New York: van Nostrand, 1957.
- [431] SUPPES, P. Models of Data. In NAGEL, E; SUPPES, P; TARSKI, A (eds.). Logic Methodology and the Philosophy of Science: Proceedings of the 1960 International Congress. Stanford, CA: Stanford University Press, 1962, 252-261.
- [432] SUPPES, P. What is a Scientific Theory?. In MORGENBESSER, S. (Ed.). Philosophy of Science Today. New York: Basic Books, 1967, 55-67.
- [433] SUPPES, P. Set theoretic Structures in Science. Stanford: Stanford University Press, 1967.
- [434] SUPPES, P. Some Remarks about Complexity. Philosophy of Science Association, 1977, 2, 543-547.
- [435] TAYLOR, R. Causation. In Encyclopedia of Philosophy, P. Edwards, Macmillan, New York, 1967.
- [436] TEMPERLY, HNV. Graph Theory and Applications. Chichester: Ellis Horwood, 1981.
- [437] TIAN, J; ZELKOWITZ, V. Complexity Measure Evaluation and Selection. IEEE Transactions on Software Engineering, 1995, 21, 641-650.
- [438] TOULMIN, S. The Philosophy of Science. London: Hutchinson, 1953.
- [439] TRAPPL, R (Ed.). Power, Autonomy, Utopia: New Approaches towards Complex Systems. New York: Plenum Press, 1986.
- [440] TRAUB, JF; WASILKOWSKI, GW; WOZNIAKOWSKI, H. Information, Uncertainty, Complexity. Reading, MA: Addison-Wesley, 1983.
- [441] TRAUB, JF; WASILKOWSKI, GW; WOZNIAKOWSKI, H. Information-Based Complexity. London: Academic Press, 1988.
- [442] TRAUB, JF; WOZNIAKOWSKI, H. Information-Based Complexity: New Questions for Mathematicians. Mathematical Intelligencer, 1991, 13, 34-43.
- [443] TURING, AM. On computable Numbers with an Application to the Entscheidungsproblem. Proceedings of the London Mathematical Society, 1936, 42, 230-265.
- [444] TURNEY, P. The Architecture of Complexity: A new blueprint. Synthese, 1989, 79, 515-542.

- [445] TURNEY, P. Problems with Complexity in Gold's Paradigm of Induction-Part I: Dynamic Complexity. *International Journal of General Systems*, 1990, 17, 329-342.
- [446] TURNEY, P. Problems with Complexity in Gold's Paradigm of Induction--Part II: Static Complexity. *International Journal of General Systems*, 1990, 17, 343-358.
- [447] TURNEY, P. The Curve Fitting Problem: A Solution. *British Journal for the Philosophy of Science*. 1990, 41, 509-530.
- [448] ULRICH, D. The Shortest Possible Length of the Longest Implicational Axiom. *Journal of Philosophical Logic*, 1996, 25, 101-108.
- [449] USPENSKY, VA. Kolmogorov and mathematical Logic. *Journal for Symbolic Logic*, 1992, 57, 385-411.
- [450] VAN EMDEN, MH. An Analysis of Complexity. *Mathematical Centre Tracts 35*, Mathematisch Centrum Amsterdam, Amsterdam, 1971
- [451] VAN LAMBAGEN, M. Algorithmic Information Theory. *Journal for Symbolic Logic*, 1989, 54, 1389-1400.
- [452] DE VANY, A. Information, Bounded Rationality, and The Complexity of Economic Organisation. Discussion paper, Dept. of mathematics, University. of California, 1993.
- [453] VITUSHKIN, AG. Theory of Transmission and Processing of Information. New York: Pergamon Press, 1961.
- [454] VON NEUMANN, J. Theory of Self-Reproducing Automata. Urbana, Illinois: University of Illinois Press, 1966.
- [455] VRANCKX, A. Narratives of "evolution", "systems" and "complexity" – Semantic interpretations of realities and representation. In AERTS, D (ed.). *University and Society - Social and Cultural Studies of the Sciences*. Kluwer, Amsterdam, 1996.
- [456] VYUGIN, VV. On the Defect of Randomness of a Finite Object with respect to Measures with given Complexity Bounds. *Theory of Probability and its Applications*, 1988, 32, 508-512.
- [457] WACKERBAUER, R; WITT, A; ALTMANSPRACHER, H; et al. A Comparative Classification of Complexity Measures based on distinguishing partitions in phase space as well as structural v. dynamic elements. *Chaos, Solitons and Fractals*, 1994, 4, 133-173.
- [458] WALKER, CC. Behaviour of a Class of complex systems: The effect of systems size on properties of terminal cycles. *Journal of Cybernetics*, 1971, 1, 55-67.
- [459] WARFIELD, JN. Planning, Policy, and Complexity. New York: Wiley, 1976.
- [460] WARFIELD, JN. An Essay On Complexity. Centre for Advanced Study in the Integrative Sciences Report, Institute of Public Policy, George Mason University, Virginia, US, 1995.

- [461] WARFIELD, JN. Laws of Complexity. Center for Advanced Study in the Integrative Sciences Report, Institute of Public Policy, George Mason University, Virginia, US, 1996.
- [462] WARTOFSKY, MW. Models. Boston Studies in the Philosophy of Science, Vol. 129. Dordrecht: Reidel, 1979.
- [463] WAXMAN, M. Problem Complexity. Available electronically at URL: <http://www.fmb.mmu.ac.uk/~bruce/waxman.txt>, 1996.
- [464] WEAVER, W. Science and Complexity. American Scientist, 1948, 36, 536-544.
- [465] WEISS, L. Statistical Decision Theory. New York: McGraw-Hill, 1961.
- [466] WEYUKER, EJ. The Evaluation of Software Complexity Measures. IEEE Transactions on Software Engineering, 1988, 14, 1357-1365.
- [467] WHITEHEAD, AN; RUSSELL, B. Principia Mathematica. Cambridge: Cambridge University Press, 1910.
- [468] WIMSATT, W. Complexity and Organisation. In SCHAFFNER, K; COHEN, R (Eds). Studies in the Philosophy of Sciences. Dordrecht: Reidel, 1972, 67-86.
- [469] WINNIE, JA. Computable Chaos. Philosophy of Science, 1992, 59, 263.
- [470] WINOGRAD, S. Redundancy and Complexity of Logical Elements. Information and Control, 1963, 5, 177-194.
- [471] WOLFRAM, S. Cellular Automata as Models of Complexity. Nature, 1984, 311, 419-424.
- [472] WOLFRAM, S. Computational Theory of Cellular Automata. Communications in Mathematical Physics, 1984, 96, 15-57.
- [473] WOLFRAM, S. Universality and Complexity in Cellular Automata. Physica D, 1984, 10, 1.
- [474] WOLFRAM, S. Origins of Randomness in Physical Systems. Physics Review Letters, 1985, 55, 449-452.
- [475] WOLFRAM, S (Ed.). Theory and Applications of Cellular Automata. Singapore: World Scientific, 1986.
- [476] WOLFRAM, S. Complex Systems Theory. In PINES, D (Ed). Emerging Syntheses in Science. Redwood City, California: Addison-Wesley, 1987, 183-190.
- [477] WOOD, RE. Task Complexity: definition of the construct. Organisational Behaviour and Human Decision Processes, 1986, 36, 60-82.
- [478] WOODWARD, D. Understanding Complexity: A Critique and Synthesis. Henley-on-thames: Henley Management College, 1992.

- [479] WOODS, J. Relevance. *Logique et Analyse*, 1996, 27, 130-137.
- [480] XIE, H. Distinct Excluded Blocks and Grammatical Complexity of Dynamical Systems. *Complex Systems*, 1995, 9, 73-90.
- [481] YATES, FE. Complexity and the limits to knowledge. *American Journal of Physiology*, 1978, 235, R201-R204.
- [482] YATES, FE. Order and Complexity in Dynamical Systems - Homeodynamics as a Generalised Mechanics for Biology. *Mathematical and Computer Modelling*, 1994, 19, 49-74.
- [483] YNGVE, VH. A model and an hypothesis for language structure. *Proceedings of the American Philosophical Society*, 1960, 104, 444-466.
- [484] YOKOYAMA, T. Complexity and Hierarchy Theory. *Osaka Economic Papers*, 1976, 26, 26-34.
- [485] YOUNG, P; PARKINSON, S; LEES, M. Simplicity out of complexity in environmental modelling: Occam's razor revisited. *Journal of Applied Statistics*, 1996, 23, 165-210.
- [486] YUDIN, D; GORYASHKO, A. Control problems and Complexity Theory I. *Engineering Cybernetics*, 1974, 12, 10-24.
- [487] YUDIN, D; GORYASHKO, A. Control problems and Complexity Theory II. *Engineering Cybernetics*, 1975, 13, 1-13.
- [488] ZADEH, LA. Outline of a new approach to the analysis of complex systems and decision processes. *IEEE Transactions on Systems, Man and Cybernetics*, 1973, 3, 28-44.
- [489] ZADEH, LA. Coping with the imprecision of the real world. In YAGER, RR et al. (eds.). *Selected Papers by Lofti A. Zadeh*. New York: John Wiley, 1987, 9-28.
- [490] ZAMBELLA, D; GRASSBERGER, P. Complexity of Forecasting in a Class of Simple Models. *Complex Systems*, 1988, 2, 269-303.
- [491] ZEIGARNIK, AV; TEMKIN, ON. A graph-theoretic model of complex reaction mechanisms: a new complexity index for reaction mechanisms. *Kinetics and Catalysis*, 1996, 37, 372-385.
- [492] ZEIGLER, BP. Simulation based structural complexity of models. *International Journal of General Systems*, 1976, 2, 217-223.
- [493] ZHANG, B-T; MÜHLENBEIN, H. Balancing accuracy and parsimony in genetic programming. *Evolutionary Computation*, 1995, 3, 17-38.
- [494] ZIMAND, M. A High-Low Kolmogorov Complexity Law equivalent to the 0-1 Law. *Information Processing Letters*, 1996, 57, 59-64.

[495] ZIV, J. Complexity and Coherence of Sequences. In DURAND, H; DI LULLO, M; SINCLAIR, C (Eds). The Impact of Data Processing Techniques on Communications. Dordrecht: Nijhoff, 1983, 23-33.

[496] ZUREK, WH. Algorithmic Randomness and Physical Entropy. Physics Review A, 1989, 40, 4731-4751.

[497] ZUREK, WH. Algorithmic Information Content, Church-Turing Thesis, Physical Entropy, and Maxwell's Demon. In ZUREK, WH (Ed). Complexity, Entropy and the Physics of Information. Redwood City, California: Addison-Wesley, 1990, 73-89.

[498] ZUSE, H. Software Complexity. Berlin: Walter de Gruyter, 1991.

[499] ZVONKIN, AK; LEVIN, LA. The Complexity of Finite Objects and the Development of the Concepts of Information and Randomness by Means of the Theory of Algorithms. Russian Mathematics Surveys, 1970, 256, 83-124.

[500] ZWIETERING, PJ; AARTS, EHL; WESSELS, J. Design and Complexity of Exact Multi-Layered Perceptrons. International Journal of Neural Systems, 1994, 2, 185-201.

Bibliography

Mr. Couture received a B.Sc. degree in Physics and a M.Sc. in Physical Oceanography at the Université du Québec à Rimouski, Qc, Canada. After 8 years of M&S work at Fisheries and Ocean Canada, he completed a M.Sc. in Electrical Engineering at Laval University, Qc, Canada. In 2002, he joined Defence R&D Canada - Valcartier as a Defence Scientist in the Systems Engineering and Architecture (SEA) Group, which is part of the System of Systems (SoS) Section. His research interests are oriented toward the study, design and engineering of military complex systems through the lens of the Complexity Theory.

Distribution list

Document No.: DRDC Valcartier TN 2006-451

LIST PART 1: Internal Distribution by Centre:

- 1 Guy Turcotte (SdS)
- 1 Michel Ducharme (SdS)
- 1 Robert Charpentier (GIC)
- 1 Éloi Bossé (SAD)
- 1 Yves Van Chestein (GIC)
- 1 Mario Couture
- 3 Bibliothèque

9 TOTAL LIST PART 1

LIST PART 2: External Distribution by DRDKIM

DRDKIM (pdf)

0 TOTAL LIST PART 2

9 TOTAL COPIES REQUIRED

This page intentionally left blank.

DOCUMENT CONTROL DATA

(Security classification of title, body of abstract and indexing annotation must be entered when the overall document is classified)

1. ORIGINATOR (The name and address of the organization preparing the document. Organizations for whom the document was prepared, e.g. Centre sponsoring a contractor's report, or tasking agency, are entered in section 8.)		2. SECURITY CLASSIFICATION (Overall security classification of the document including special warning terms if applicable.)	
Defence R&D Canada – Valcartier 2459 Pie-XI Blvd North Quebec (Quebec) G3J 1X5 Canada			
3. TITLE (The complete document title as indicated on the title page. Its classification should be indicated by the appropriate abbreviation (S, C, R or U) in parentheses after the title.)			
Complexity and Chaos - State-of-the-Art; Formulations and Measures of Complexity:			
4. AUTHORS (last name, followed by initials – ranks, titles, etc. not to be used)			
Couture Mario			
5. DATE OF PUBLICATION (Month and year of publication of document.)	6a. NO. OF PAGES (Total containing information, including Annexes, Appendices, etc.)	6b. NO. OF REFS (Total cited in document.)	
September 2007	62	9 + 500 from Edmonds (1999)	
7. DESCRIPTIVE NOTES (The category of the document, e.g. technical report, technical note or memorandum. If appropriate, enter the type of report, e.g. interim, progress, summary, annual or final. Give the inclusive dates when a specific reporting period is covered.)			
Technical Note			
8. SPONSORING ACTIVITY (The name of the department project office or laboratory sponsoring the research and development – include address.)			
Section: Information and Knowledge Management. Address: Defense R&D Canada, DRDC-Valcartier, 2459, boul. Pie-XI nord, Québec, Canada, G3J 1X5 (Robert Charpentier)			
9a. PROJECT OR GRANT NO. (If appropriate, the applicable research and development project or grant number under which the document was written. Please specify whether project or grant.)	9b. CONTRACT NO. (If appropriate, the applicable number under which the document was written.)		
15bp01 - Defensive Software Design			
10a. ORIGINATOR'S DOCUMENT NUMBER (The official document number by which the document is identified by the originating activity. This number must be unique to this document.)	10b. OTHER DOCUMENT NO(s). (Any other numbers which may be assigned this document either by the originator or by the sponsor.)		
DRDC Valcartier TN 2006-451			
11. DOCUMENT AVAILABILITY (Any limitations on further dissemination of the document, other than those imposed by security classification.)			
<input checked="" type="checkbox"/> Unlimited distribution <input type="checkbox"/> Defence departments and defence contractors; further distribution only as approved <input type="checkbox"/> Defence departments and Canadian defence contractors; further distribution only as approved <input type="checkbox"/> Government departments and agencies; further distribution only as approved <input type="checkbox"/> Defence departments; further distribution only as approved <input type="checkbox"/> Other (please specify):			
12. DOCUMENT ANNOUNCEMENT (Any limitation to the bibliographic announcement of this document. This will normally correspond to the Document Availability (11). However, where further distribution (beyond the audience specified in (11) is possible, a wider announcement audience may be selected.)			

13. **ABSTRACT** (A brief and factual summary of the document. It may also appear elsewhere in the body of the document itself. It is highly desirable that the abstract of classified documents be unclassified. Each paragraph of the abstract shall begin with an indication of the security classification of the information in the paragraph (unless the document itself is unclassified) represented as (S), (C), (R), or (U). It is not necessary to include here abstracts in both official languages unless the text is bilingual.)

Different formulations and measures that may be used for evaluating the complexity of systems are gathered in this Technical Note. They might be useful for describing aspects of military complex systems. They were extracted from documents issued from the scientific literature related to Complexity Theory, chaos and complex systems.

Différentes formulations et mesures qui peuvent être utilisées pour évaluer la complexité des systèmes sont rassemblées dans ce document. Ces formulations et mesures peuvent être utiles pour décrire différents aspects des systèmes militaires complexes. Elles ont été extraites de documents provenant de la littérature scientifique traitant de la théorie de la complexité, du chaos et des systèmes complexes.

14. **KEYWORDS, DESCRIPTORS or IDENTIFIERS** (Technically meaningful terms or short phrases that characterize a document and could be helpful in cataloguing the document. They should be selected so that no security classification is required. Identifiers, such as equipment model designation, trade name, military project code name, geographic location may also be included. If possible keywords should be selected from a published thesaurus, e.g. Thesaurus of Engineering and Scientific Terms (TEST) and that thesaurus identified. If it is not possible to select indexing terms which are Unclassified, the classification of each should be indicated as with the title.)

Complexity, formulations, descriptions, measures, metric, theory, theories, concepts, complex, systems.

Defence R&D Canada

Canada's Leader in Defence
and National Security
Science and Technology

R & D pour la défense Canada

Chef de file au Canada en matière
de science et de technologie pour
la défense et la sécurité nationale



WWW.drdc-rddc.gc.ca

